

Master M2 EEET - EDDEE - *Module Economie de la Forêt et du bois*

Modélisation de la filière forestière française (FFSM)

Modelling

- Forest Sector Modelling
- French Forest sector Modelling



SCAN ME

<https://bit.ly/ffsm2023>

Antonello Lobianco

“Weather forecast for tonight: dark.”

-- George Carlin, American comedian

Today's objectives

Understand how the complex interactions of the (French) Forest sector, linking forest dynamics, people pursuit's of own goals, markets "behaviours" and society objectives for a better environment, can be accounted, represented and modelled.

Modelling

Forest sector modelling

The French Forest Sector Model

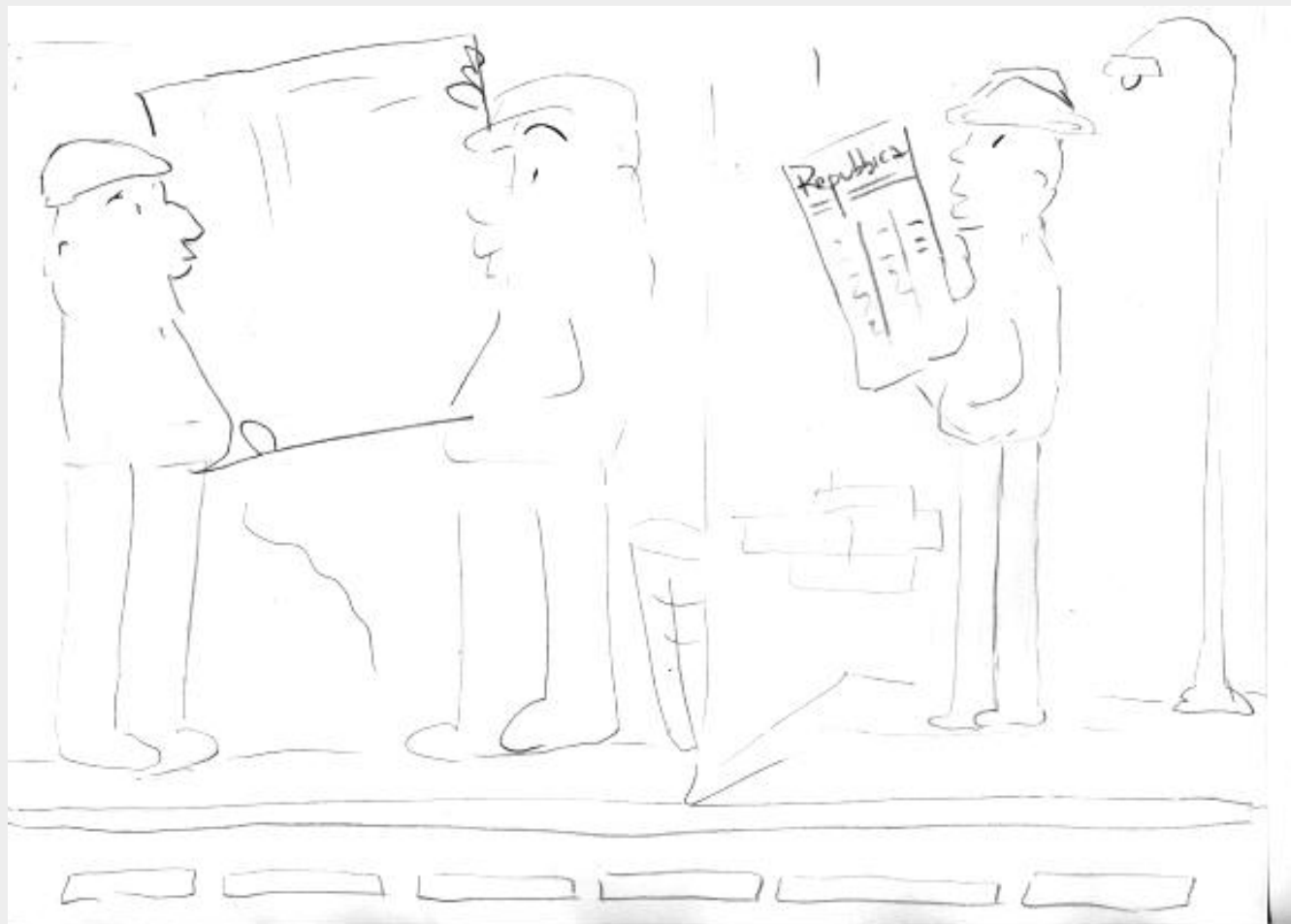
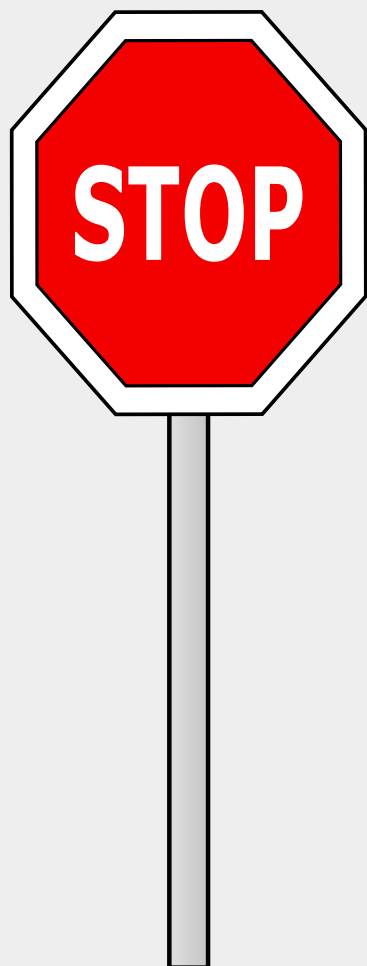
- **Forest resources dynamics**
 - recognition of forest diversity
 - path dependency
 - environmental changes
- **HWP markets**
 - supply, demand, trade
 - price transmission channels
- **Forest investments decisions**
 - how we model individual forest owners
- **Climate change**
 - cc effects on the forest (already seen)
 - do forests really mitigate climate change ?
 - implementation of a carbon module



MODELLING

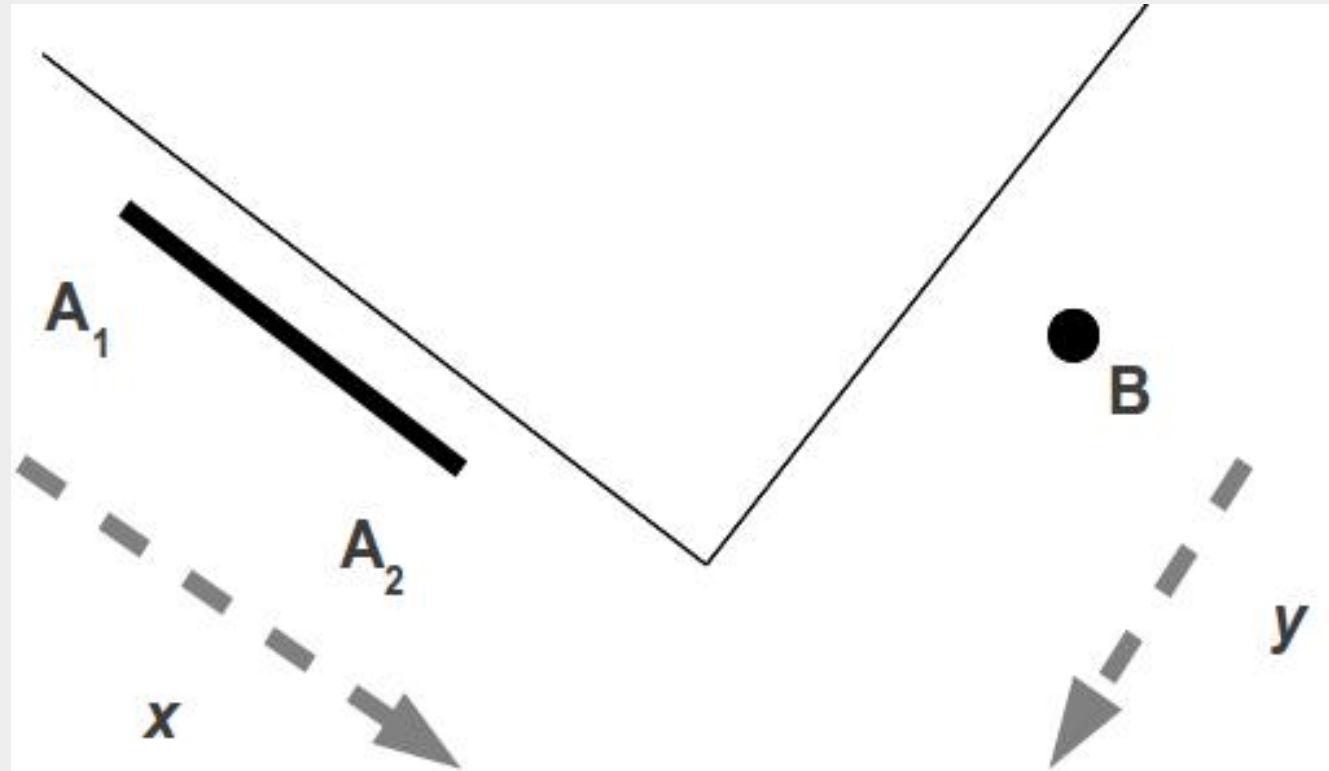
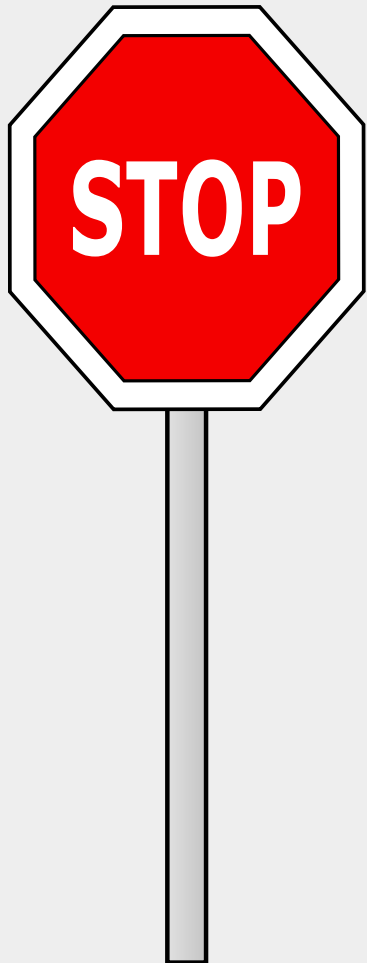
First step.. what is a *model* ??

Reality → model → math. form.



First step.. what is a *model* ??

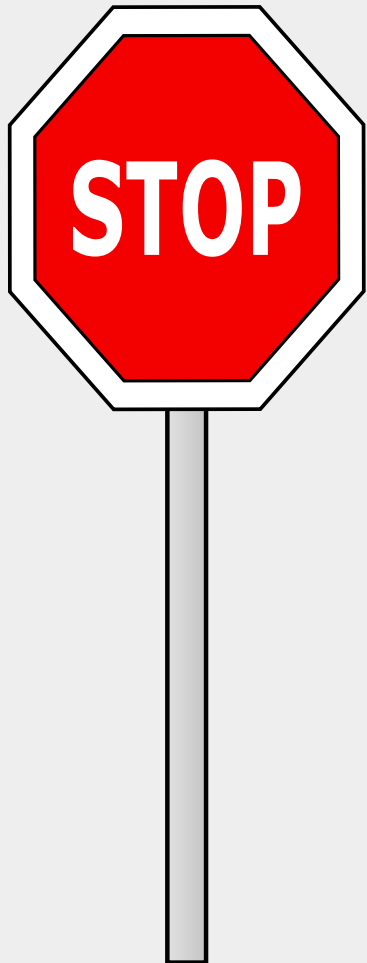
Reality \rightarrow model \rightarrow math. form.



A model is useful if it helps us to answer a research question, in this case if a crash will happen.

First step.. what is a *model* ??

Reality → model → math. form.



We need to define which elements to retrain from our observation of the reality (inductive reasoning), which assumptions to make and which data we need, and which reasoning to apply (deductive part) in order to answer the research question.

Info needed:

$x_{A1}, x_{A2}, y_B, v_A, v_B$

Assumptions:

v_A, v_B constant

Model:

physical space/time/speed relation



First step.. what is a *model* ??

Reality \rightarrow model \rightarrow math. form.

$$t_{A1} = \frac{x_{A1}}{v_A} \quad t_{A2} = \frac{x_{A2}}{v_A} \quad t_B = \frac{y_B}{v_B}$$

crash iff $t_{A2} \leq t_B \leq t_{A1}$



Implementation in Julia

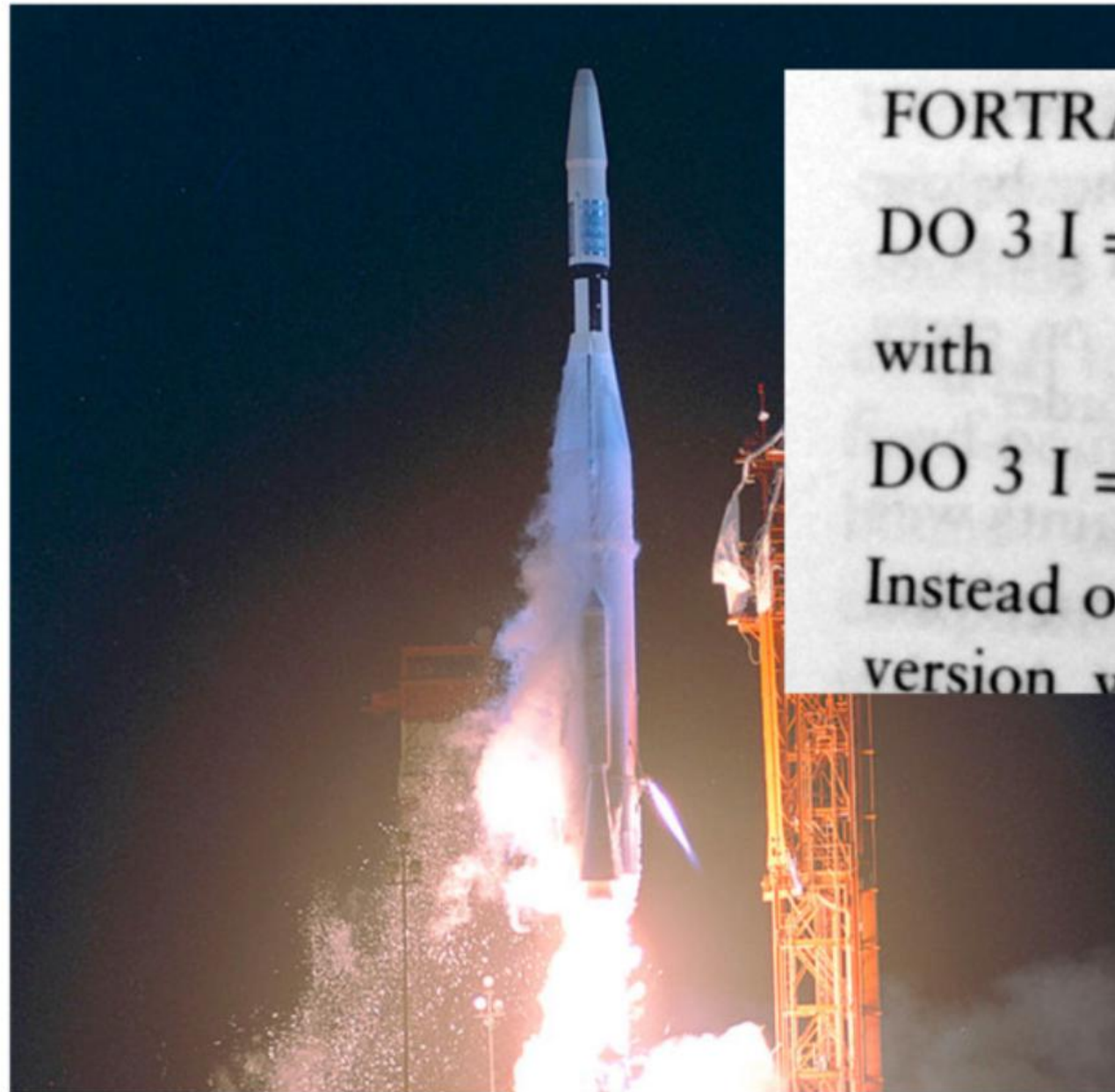
- Download and doc: <https://julia.org>
- Run online: <https://juliabox.com>
- Tutorial: <https://www.gitbook.com/book/sylvaticus/julia-language-a-concise-tutorial/details>

```
function determineClash(xa1, xa2, yb, va, vb)
    ta1 = xa1/va
    ta2 = xa2/va
    tb = yb/vb
    if (ta2 <= tb <= ta1)
        return true
    else
        return false
    end
end
```

```
determineClash(8, 5, 12, 3, 6) # true
determineClash(8, 5, 12, 3, 4) # false
```

Models can be “wrong” in both the translation of elements that matter in the modelling idea (assumptions) or in their formalisations (e.g. Mariner 1, 1962 satellite, Mars Climate Orbiter 1998)

Programming is error-prone



FORTTRAN statement

```
DO 3 I = 1,3
```

with

```
DO 3 I = 1.3
```

Instead of looping thro
version would be

Mariner 1
1962

F...A...I...L...U...R...E... (Famous bugs)

- Mars Climate Orbiter (1998)
 - \$655M space probe crashes due to wrong units system.





FOREST SECTOR MODELLING

Which are the distinctive elements of the forest sector

- Why "forest economics" ?

- Strong link resource markets
 - wood (still) much less global than cotton, steel
 - Depends on the product: hardwood >> softwood >> industrial wood (e.g. Clairefontaine)
 - strong link with the spatial dimension
- Bounded ownerships rights, externalities, call for public policies:
 - optimal production of public goods
 - (optimal consumption of common resources)
- Very long investment (→ hazard)
- At the same time strongly influenced by climate change and a possible source of its mitigation (the "loop effect")
- Still an "important" sector in France (especially locally):
 - 3.3 M + 270 m people
 - 12 b€, 0.6% GDP

Who are the agents involved in the forest sector ?

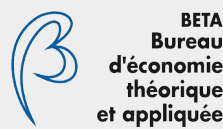
- Forest Owners (→ Managers, owner unions)
- Wood sector agents (→ Unions, commerce bodies)
- Citizens (→ Gov and not gov. organisations)

Which are the research questions ?

- Forest Owners
 - Timber production optimisations (optimal rotation, optimal choice of species);
 - Climate change adaptation;
 - Risk management (assurance, forest management changes, risk diversification - portfolio, ...)
 - Understand non-market benefits (and behaviour)
- Wood sector agents
 - Timber markets effect: producer's surplus, added value, trade balance, jobs
- Citizens
 - Consumer's surplus
 - Demand of ecosystem-services, production possibility frontier
 - Carbon mitigation

While we may have different research questions, some of the underlying assumptions/logic may be in common

→ May have sense to have a modelling framework where to "plug" a specific model tailored to the research question



THE FRENCH FOREST SECTOR MODEL

French Forest Sector Model (FFSM)

The screenshot shows the website for the French Forest Sector Model (FFSM++) in English. The browser address bar shows the URL `ffsm-project.org/wiki/en/home`. The website header includes logos for INRA and AgroParisTech, and identifies the model as being developed by the Laboratoire d'Economie Forestière (LEF) in Nancy, France. A navigation menu on the left lists sections like Home, Documentation, Team, Development, and the laboratory name. The main content area features a search bar and links for 'Download FFSM++', 'Browse source code', 'Open a support request or bug ticket', and 'Intranet (private area)'. A central window titled 'FFSM - Forest Sector Simulator' is open, displaying a map of France with forest areas highlighted in green. A log window on the right shows the simulation's progress, including messages like 'Starting cashing on pixel spatial-level exogenous data' and 'Running optimisation problem for this year'. At the bottom of the screenshot is a flowchart illustrating the model's components: 'Climate scenario' feeds into 'Area Allocation module' (1 - future growth and mortality expectations) and 'Forest dynamics module' (1 - growth, mortality). The 'Area Allocation module' also feeds into 'Forest resources' (5 - regeneration area). 'Forest resources' feeds into 'Markets module' (2 - available volumes) and 'Forest managers' (4 - harvested area). 'Forest managers' feeds into 'Area Allocation module' (3 - harvested area). 'Markets module' feeds into 'Forest resources' (3 - harvesting volumes) and 'Wood products markets'.

Which kind of research questions we aim to answer?

- Forest Owners
 - Optimal investment choice in a spatially explicit, evolving context
 - Their preferences are input for us
 - Not at the individual level
- Wood sector agents
 - Timber markets effect: added value, trade balance, jobs
 - Perennity of the resource
 - Optimal location / resource impact of wood transformation industries
- Citizens
 - Consumer's surplus
 - Carbon mitigation outcomes

Implementation

- FFSM development

- Multidisciplinary team at the Bureau d'Economie Théorique et Appliquée BETA
- Under continuous development since 2010
- Several PhD cycles (but few students touch the code)

Current Team

- Ahmed Barkaoui
- Felix Bastit
- Sylvain Caurla
- Philippe Delacote
- Antonello Lobianco
- Claire Montagné-Huck
- Alexandra Niedzwiedz
- Miguel Rivière
- David Shanafelt

Past members

- Julien Barthès
- Thomas Beaussier
- Iason Diafas
- Frank Lecocq
- Etienne Lorang
- Claudio Petucco
- Alexandre Sauquet

External contributors

- Jean-Daniel Bontemps (SILVA)
- Hélène Chevalier (IGN)
- Antoine Colin (IGN)
- Pierre Mérian (IGN)
- Holger Wernsdörfer (SILVA)

Implementation

- development

The screenshot shows the Qt Creator IDE with the following components:

- Left Panel:** Project Explorer showing the file structure of the 'ffsm' project, including folders like 'Sources' and files like 'ModelCoreSpatial.cpp'.
- Editor:** Displays the code for 'ModelCoreSpatial.cpp'. The current function is `ModelCoreSpatial::runInitPeriod()`, which contains several commented-out lines and a `runSimulationYear()` function.
- Right Panel:** Variable Inspector showing a list of variables and their values, such as `MD` (0x831), `WL2` (99999), and `secondYear` (2006).
- Bottom Panel:** Debug Console showing a stack trace. The current thread is #1, stopped at breakpoint 1 (1) in thread 1. The stack trace includes:

Level	Function	File	Line	Number	Function	File	Line	Address
0	ModelCore...	ModelCore...	32	1	ModelCore...	/home/lobi...	32	0x80e5
1	Init::setInitL...	Init.cpp	137	3	ModelCore...	/home/lobi...	40	0x80e5
2	Init::setInitL...	Init.cpp	58	4	ModelCore...	/home/lobi...	49	0x80e5
3	MainProgra...	MainProgra...	88	5	Opt::declar...	/home/lobi...	63	0x808b

Implementation

- development

- **GAMS version**

- code: <https://github.com/LEFNancy/ffsm>
- included modules: forest dynamics, mkt, (basic) area allocation
- requires: gams, excel

- **C++ version (Desktop GUI/ command line)**

- code: https://github.com/LEFNancy/ffsm_pp
- included modules: forest dynamics (spatial), mkt, area allocation, carbon module, pathogen module
- requires:
 - Linux: Qt5, Ipopt+ADOL-C+Colpack stack (all open source libraries)
 - Windows: MinGW, Qt5, optional Ipopt+ADOL-C+Colpack stack (all open source libraries)

- **Julia version**

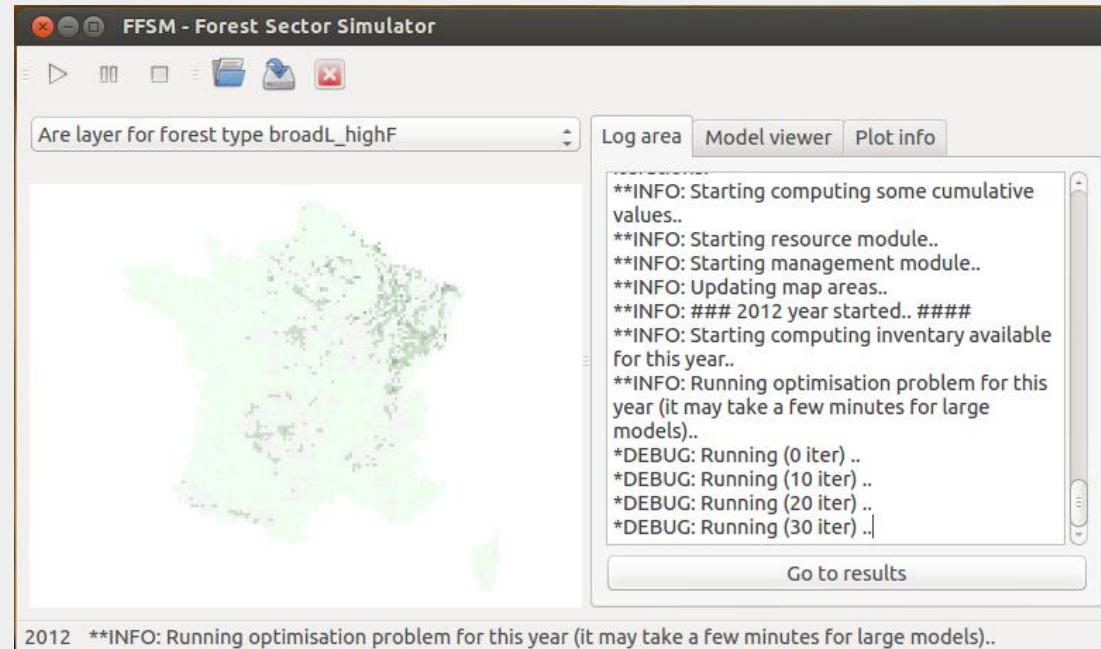
- code: <https://github.com/LEFNancy/ffsm>
- included modules: forest dynamics, mkt
- requires: Julia, libreoffice

Detailed development instructions on:

<https://ffsm-project.org/wiki/en/dev/development>

Implementation

- running scenarios



- Scenario-specific input data as LibreOffice Calc spreadsheet + simple text-based raster files
- Outputs as CSV, images and text-based rasters → analysed with ad hoc Python or Julia scripts
- Scenario run through a GUI or command line
 - 1 run, 1 century, France → ~ 1 hour, 2GB RAM
 - "debug" mode available for quicker checks
 - multiple scenarios in parallel using the `parallel` command on a simple script

Installation and usage detailed instructions:

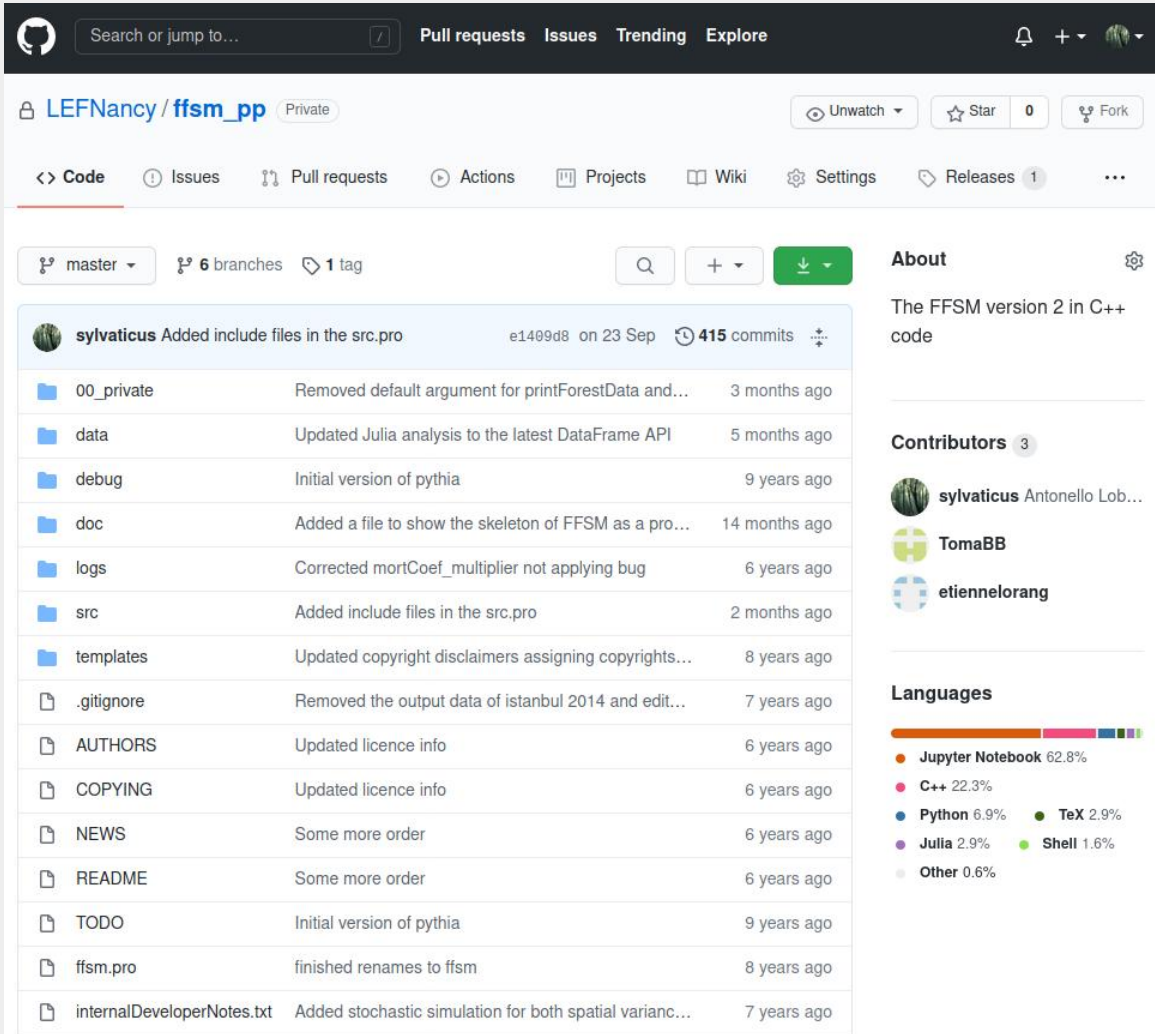
<https://ffsm-project.org/wiki/en/doc/installation>



AVAILABILITY

Availability

- source code + confidential data: private github repository:



The screenshot shows a GitHub repository page for 'LEFNancy / fsm_pp' (Private). The repository has 6 branches and 1 tag. A commit by 'sylvaticus' is highlighted, showing a list of files and folders. A red arrow points to the '00_private' folder in this list.

File/Folder	Description	Time
00_private	Removed default argument for printForestData and...	3 months ago
data	Updated Julia analysis to the latest DataFrame API	5 months ago
debug	Initial version of pythia	9 years ago
doc	Added a file to show the skeleton of FFSM as a pro...	14 months ago
logs	Corrected mortCoef_multiplier not applying bug	6 years ago
src	Added include files in the src.pro	2 months ago
templates	Updated copyright disclaimers assigning copyrights...	8 years ago
.gitignore	Removed the output data of istanbul 2014 and edit...	7 years ago
AUTHORS	Updated licence info	6 years ago
COPYING	Updated licence info	6 years ago
NEWS	Some more order	6 years ago
README	Some more order	6 years ago
TODO	Initial version of pythia	9 years ago
fsm.pro	finished renames to fsm	8 years ago
internalDeveloperNotes.txt	Added stochastic simulation for both spatial varianc...	7 years ago

About
The FFSM version 2 in C++ code

Contributors 3

- sylvaticus Antonello Lob...
- TomaBB
- etiennelorang

Languages

Language	Percentage
Jupyter Notebook	62.8%
C++	22.3%
Python	6.9%
TeX	2.9%
Julia	2.9%
Shell	1.6%
Other	0.6%

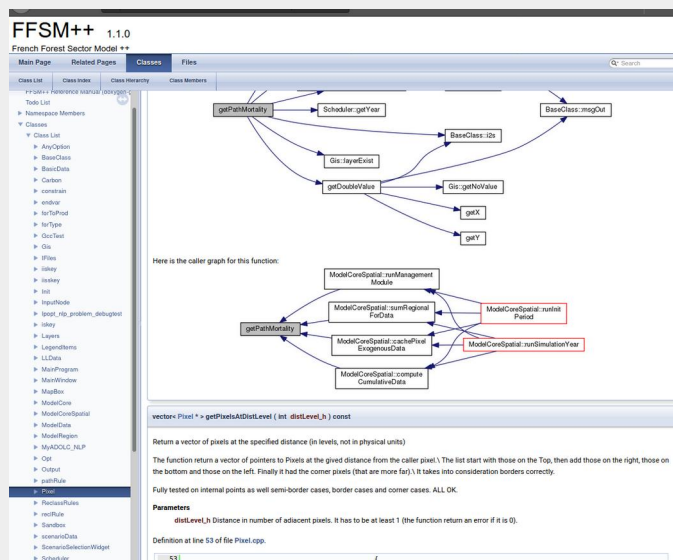
- strimmed down version (without our specific confidential projects): made available with a slightly modified GNU GPLv3 licence on a daily base

Availability

<https://ffsm-project.org/wiki/en/>

Exhaustive web site allowing the model to be discovered at different levels:

- Main mechanism, mathematical equations and theoretical foundations → academic papers
- Usage/development manuals → documentation (wiki pages)
- Detailed API → Reference Manual (automatically-generated from source code)
- Exact implementation: Source code



Given the importance of anthropogenic determinants in forest ecosystems within Europe, the objective of the FFSM++ model is to link the evidence arising from biological models with socio-economic determinants, where the expected returns of forest investments represent the main drivers.

An (inventory-based) forest dynamic model is hence coupled with a (partial equilibrium) market module and a (micro-based) management one in a national level forest sector model for France (FFSM++).

The model is fully open source (GPL3) with the sole exception that if you publish some document based on a modified version of FFSM++ you need to publish also the modifications you made. [Read the complete Licence.](#)

Documentation	Team	Usage	Development
<ul style="list-style-type: none"> Published Articles Working Papers Presentations Miscellaneous Journals of interest 	<ul style="list-style-type: none"> Current Team Past members External contributors 	<ul style="list-style-type: none"> Installation and usage instructions Development instructions Input-output data management Preparation of the spatial data (GIS layers) 	<ul style="list-style-type: none"> C++ version (FFSM++): <ul style="list-style-type: none"> Development instructions Initialisation of the market module Browse source code Reference Manual Development statistics Download latest source code Browse GIT repository (private due to some third-party copyrighted data) GAMS version: <ul style="list-style-type: none"> Browse source code (private) Download latest version (zip) (private)

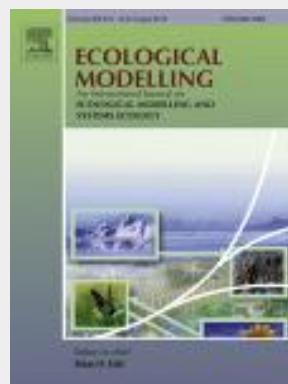
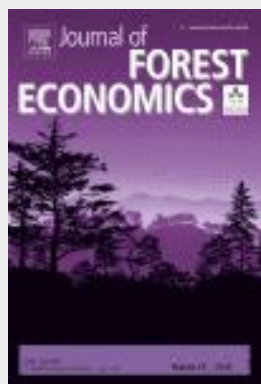


USE

Use

FFSM has been used for a wide range of analysis, of both positive and normative nature:

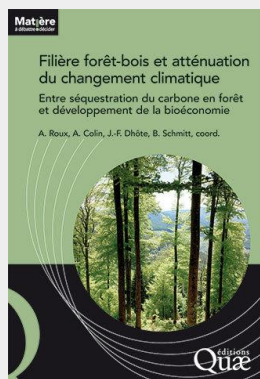
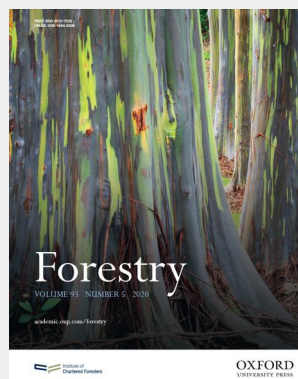
- Should policies subsidies targeted to sequestrated carbon or fuelwood ?
- Economic and resource impact of fuelwood subsidies
- Carbon tax and mitigation policies: impact on the French forest sector
- Is it better to store or export the excess of timber following large windfalls ?
- How much the future of French forests depends from human management and forest managers risk-aversion
- What is the climate change mitigation potential of the French forest sector ?
- Which is the ecological and economic effect of the introduction of the ash pathogen ?



Use (2)

FFSM has been used for a wide range of analysis, of both positive and normative nature:

- [Implications of managing forests for carbon sequestration](#)
- Impact of increased timber usage on carbon mitigation ([EN summary](#) – [FR Full Book](#))



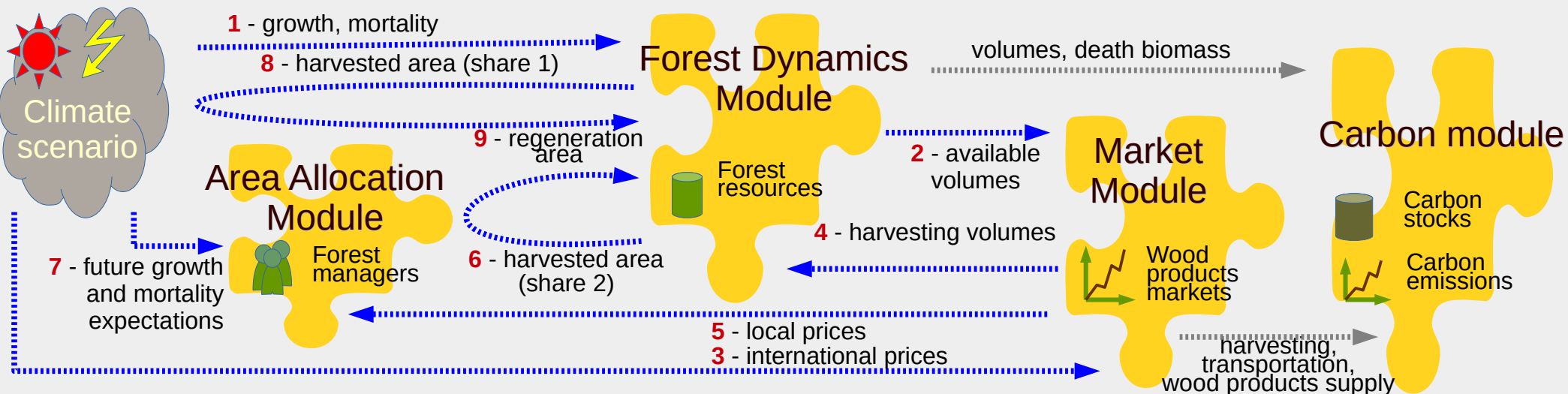
Work in progress:

- applications: implications of climate-induced changes in wildfire regimes for the forest sector and its ability to mitigate climate change; LCA assessment on a regional scale
- methodology: accounting for different behaviours small/large forest owners, private/public,...



FFSM MODULES

A modular approach

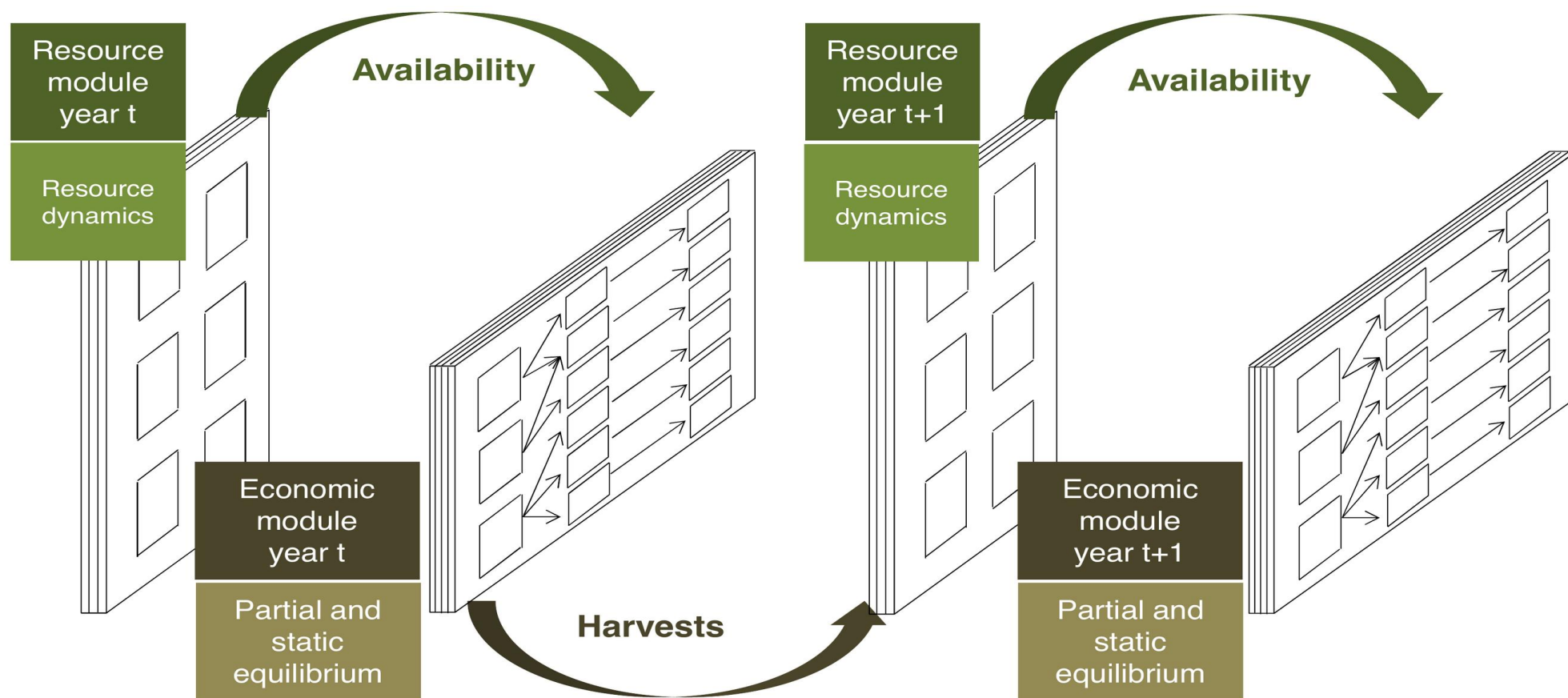


Recursive bio-economic model with coupled biological forest growth model and partial equilibrium market of forest products.

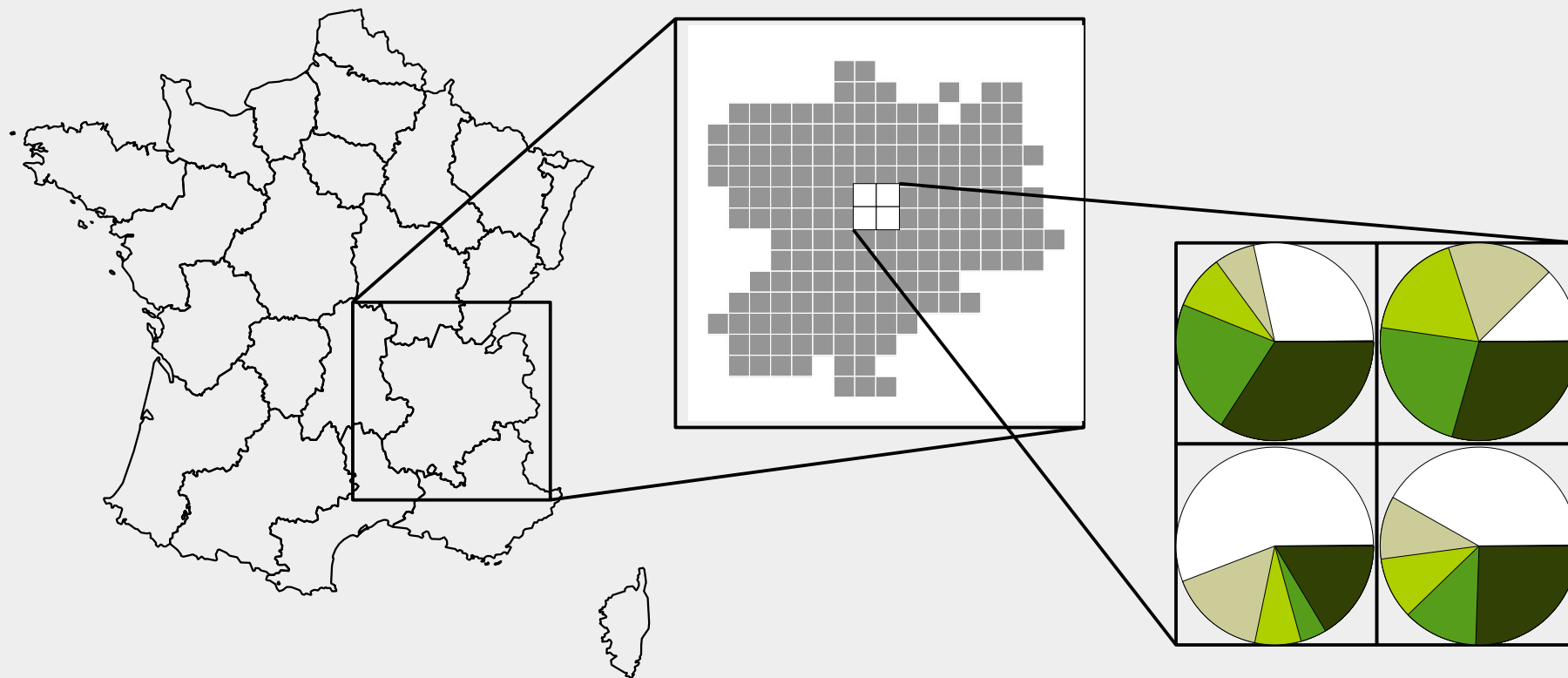
Major strength in the capacity to catch the interaction between drivers. Four interconnected modules:

- Forest dynamics module:** model forest resources
- Pathogen module:** simulation of a spatially explicit pathogen
- Market module:** HWP markets (supply, demand, trade..)
- Area allocation module:** forest investment choices
- Carbon module:** mitigation potentials of the forest sector

A recursive approach



Spatial representation



Decoupling the spatial scale of the market module (country and regional) from those of the resource and management modules (pixel level)

- regional scale reasonably adequate for the market module
- pixel level (area fraction) for resource and management model

Some notation..

- index notation

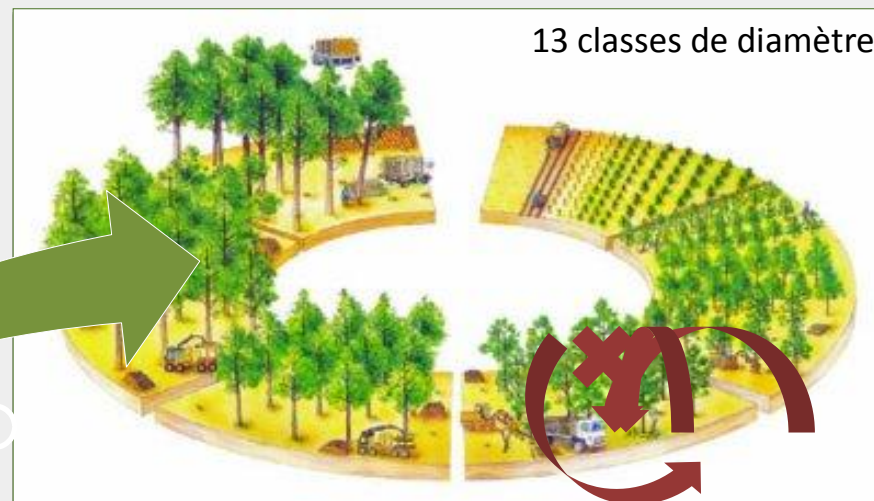
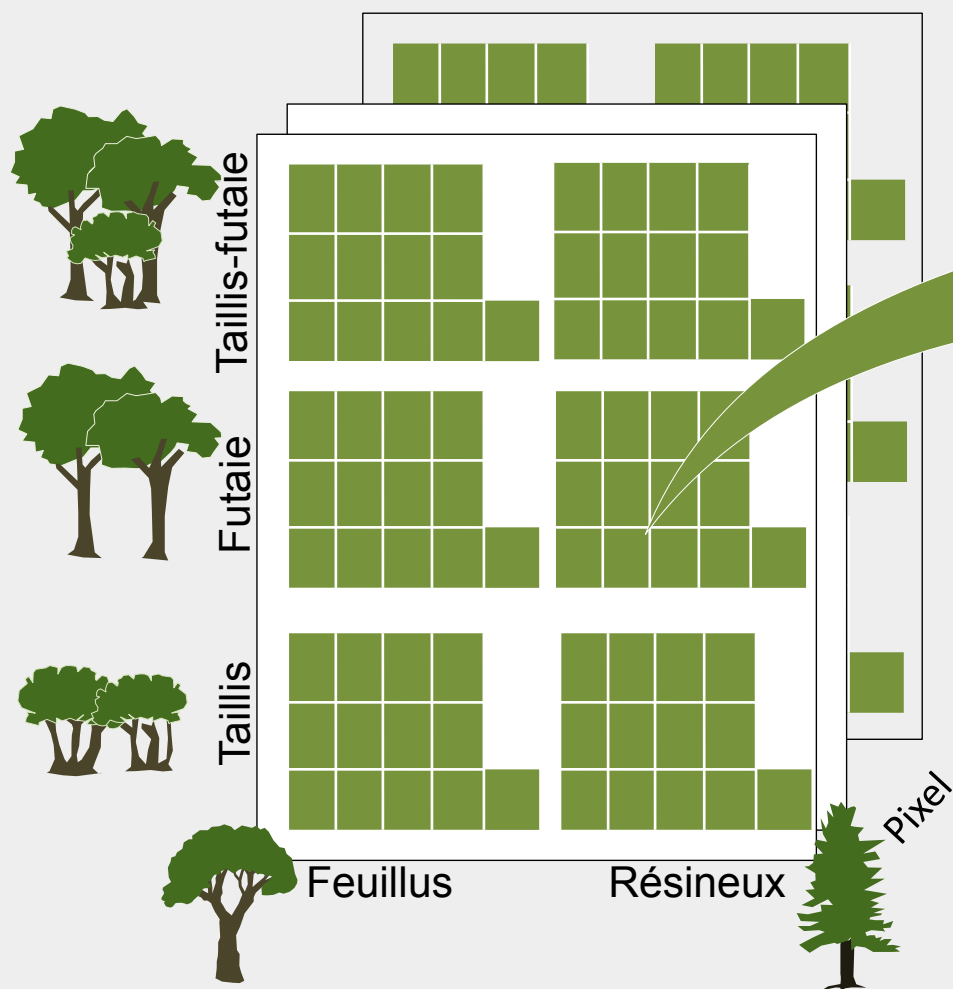
Notation	Definition	Values
t	Time	[2005 – 2100]
c	Country	{France}
r	Region	[22 administrative regions in France]
px	Pixel	8x8 km
sp	Forest species group	{Broadleaves, Coniferous}
mt	Forest management type	{High forests, Mixed forests, Coppices}
ft	Forest type (incl. mgm)	[sp × mt]
dc	Diameter class	[0,15,25...,95,150]
pp	Primary products	{Hardwood Roundwood, Softwood Roundwood, Pulpwood and Fuelwood}
tp	Transformed products	{Fuelwood, Hardwood Sawnwood, Softwood Sawnwood, Plywood, Pulpwood, Pannels}
prd	Products	[pp × tp]



FOREST RESOURCES DYNAMICS MODULE

Forest resources

- FFSM implementation (forest dynamics module)



Représentation d'un domaine d'étude (d'après dessin de Bernard Patricot CPFA)

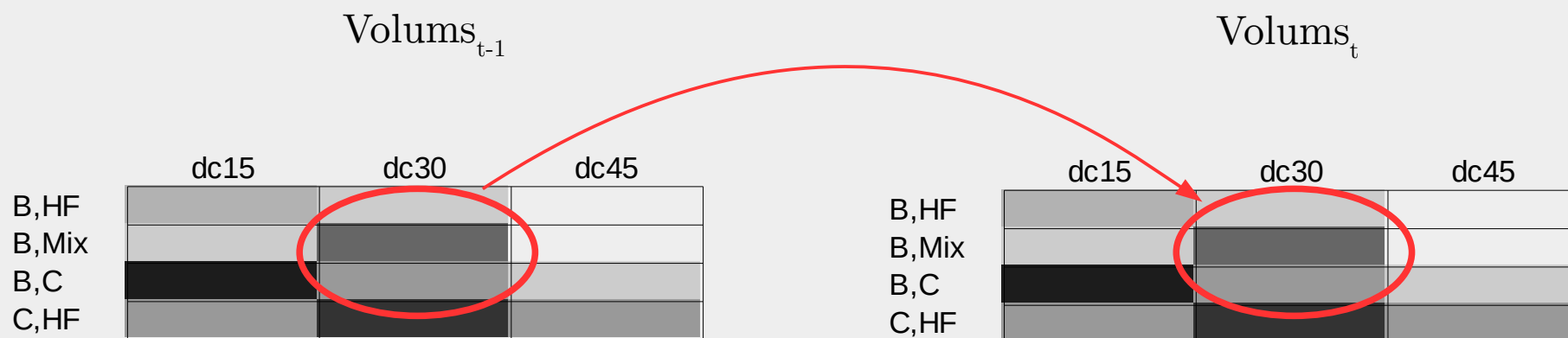
- 147 rows
- 197 cols
- 10 dc
- 4 forest types
- 1,158,360 "cells"
- State variables: volume, area
- Dynamic variables: time of passage, mortality, volume ratio, harvesting

Forest resources

- FFSM implementation (forest dynamics module)

- **Resource module:** inventory based, Markov transition matrix model, 10 diameter classes, 2 species groups (coniferous, broadleaved). From: Usher, "A Matrix Model for Forest Management", 1969.
- For each pixel (8x8 km) and forest type:

$$Vol_{dc,t} = (1 - 1/timeOfPassage_{dc,t} - mortality_{dc,t} - harvestedRate_{dc,t}) * Vol_{dc,t-1} + (1/timeOfPassage_{dc-1,t-1}) * beta_{dc} * Vol_{dc-1,t-1}$$



Forest resources

- modelling CC effect on forest resources

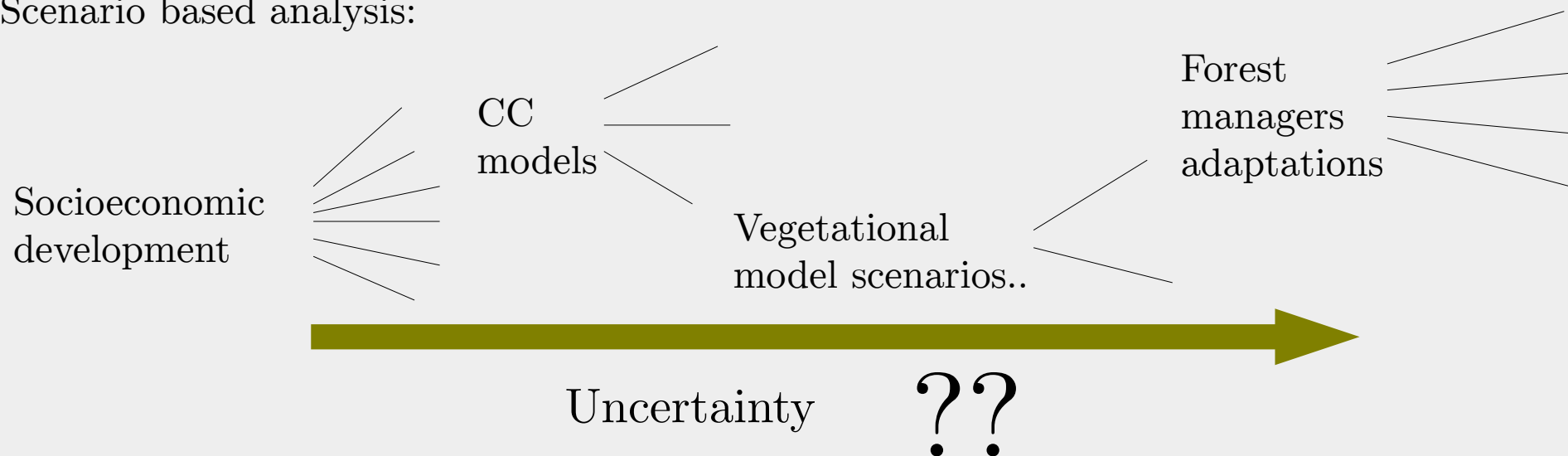
CC effects on the forest dynamics are exogenous to FFSM. Conversely, consequences on the management of the forest are explicitly accounted for.

Using *multipliers*_{sc,px,ft,t} key input biological variables can change from the regional average along the spatial and temporal dimensions according to the CC scenario under study:

- time of passage: $tp_{sc,px,ft,dc,t} = tp_{r,ft,dc,t=0} * tpMultiplier_{sc,px,ft,t}$
- mortality rate: $mort_{sc,px,ft,dc,t} = mort_{r,ft,dc,t=0} * mort_{sc,px,ft,t}$

An exogenous parameter allows the model to consider (again, exogenously) land use changes with reference to the forest (*forestChangeAreaIncrementsRel*_{sc,r,t} or *forestChangeAreaIncrementsHa*_{sc,r,t})

Scenario based analysis:





HWP MARKETS MODULE

HWP markets

- partial vs general equilibrium

Partial equilibrium models → take into consideration only a part of the market (a single product, or a sector), *ceteris paribus*, to attain equilibrium.

They assume that, on one hand, the price of every other good or the wealth one has does not change (and hence is given), and on the other hand that what happens on the market one wants to analyse has no effect on other markets.

General equilibrium models → the analysis includes an entire economy. Every market has an effect on every other market and therefore one has to model every market simultaneously.

Advantages of PEM:

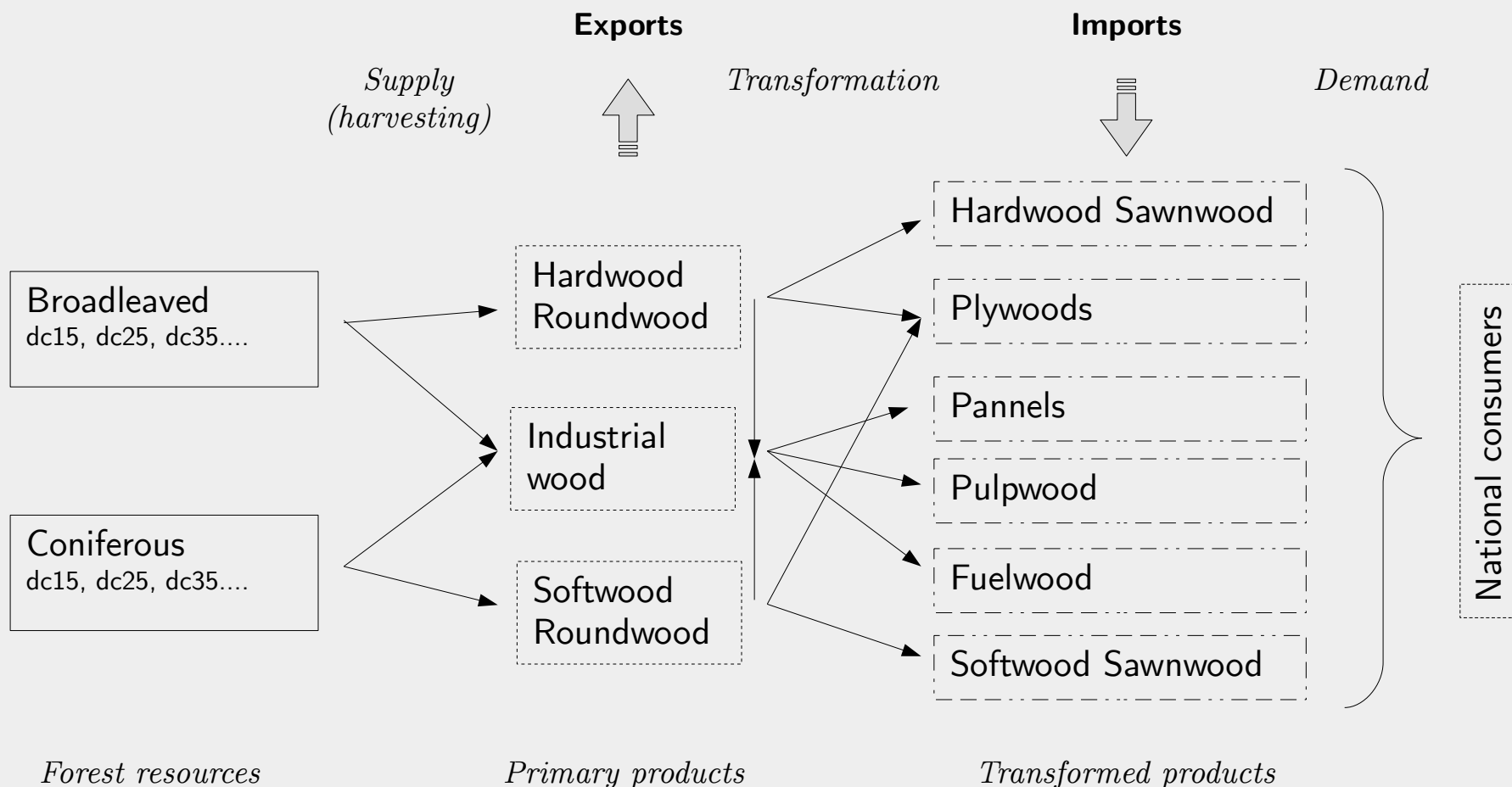
- simpler and easier to implement;
- can describe a sector in detail still guaranteeing resolution, stability and unicity of equilibrium;

Advantages of GEM:

- more realistic;
- necessary to model goods (e.g. labor, energy) that are so important, that they may have serious effects on other markets.

HWP markets

- **Market module:** partial equilibrium, 3 primary products and 6 transformed products (Leontief transformation), imperfect substitutability national vs international products, regional trade



HWP markets

- elasticity

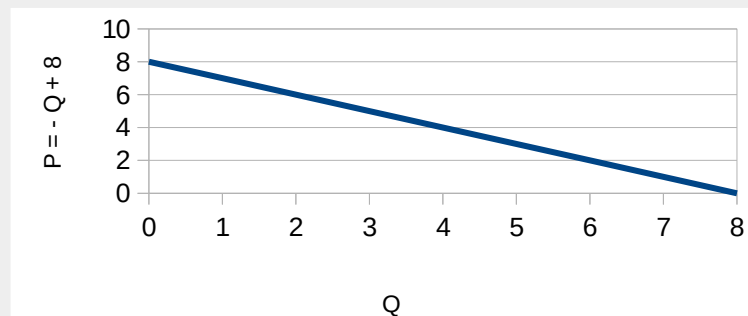
In general “elasticity of a with respect of b” means the relative change in a over a relative change in b:

$$\sigma \equiv \frac{\text{relative change in a}}{\text{relative change in b}}$$

It tells you how much something change percent when you change the other variable of one percent unit.

A simple version is for example the elasticity of demand with respect to price: with a value of, let's say, -5, it means that when you increase price of 1 percent, the demand reduces of 5 percent.

Like for simple derivatives, elasticity usually change across functions. It's only under special “constant elasticities” functions that it remains constant among the domain of the independent variable.



HWP markets

- elasticity of substitution

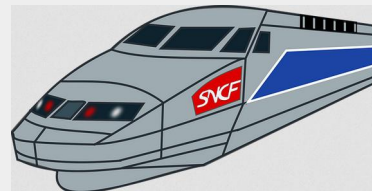
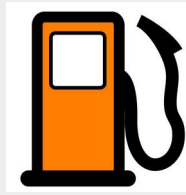
In particular, the “elasticity of substitution” measures the proportionate change in the ratio of two variables in response to a change in their relative prices.

$$\sigma \equiv \frac{\text{relative change in } (X_1/X_2)}{\text{relative change in } (P_1/P_2)} = \frac{\frac{d(X_1/X_2)}{X_1/X_2}}{\frac{d(P_1/P_2)}{P_1/P_2}}$$

$\sigma = 0$: Perfect complement goods

$0 < \sigma < \infty$: Intermediate goods

$\sigma = \infty$: Perfect substitute



HWP markets

- supply of primary products

Composite supply:

- It depends from own price and availability of the resource:
- While products in different regions are assumed perfectly homogeneous (and hence regional price depends diverge only by transport costs), national vs international products are assumed partially heterogeneous. A parameter (the Armington elasticity) defines how local prices are more or less dependant by local market condition vs external international prices:

Supply to abroad (exports):

Supply to local:

Supply value equation:

$$\frac{SC_{pp,t}}{SC_{pp,t-1}} = \left(\frac{pc_{pp,t}}{pc_{pp,t-1}} \right)^{eSP_{pp}} \left(\frac{inv_{pp,t}}{inv_{pp,t-1}} \right)^{eSI_{pp}}$$

$$S = f(p, res, k)$$

$$sc_{pp,t} = \left[(1 - tS_{pp,t}) sl_{pp,t}^{\frac{eST_{pp}-1}{eST_{pp}}} + tS_{pp,t} sa_{pp,t}^{\frac{eST_{pp}-1}{eST_{pp}}} \right]^{\frac{eST_{pp}}{eST_{pp}-1}}$$

$$sa_{pp,t} = tS_{pp,t} sc_{pp,t} * \left(\frac{pc_{pp,t}}{pa_{pp,t}} \right)^{eST_{pp}}$$

$$sl_{pp,t} = (1 - tS_{pp,t}) sc_{pp,t} * \left(\frac{pc_{pp,t}}{pl_{pp,t}} \right)^{eST_{pp}}$$

$$pc_{pp,t} sc_{pp,t} = pl_{pp,t} sl_{pp,t} + pa_{pp,t} sa_{pp,t}$$

HWP markets

- demand of transformed products

Composite demand:

- depends uniquely from the own price (but recently a cross-price elasticity has been introduced too):
- also in the demand local (national) products are assumed partially heterogeneous vs international products:

$$\frac{dc_{tp,t}}{dc_{tp,t-1}} = \left(\frac{pc_{tp,t}}{pc_{tp,t-1}} \right)^{eDP_{tp}}$$

$$dc_{tp,t} = \left[(1 - tD_{tp,t}) dl_{tp,t} \frac{eDT_{tp}-1}{eDT_{tp}} + tD_{tp,t} da_{tp,t} \frac{eDT_{tp}-1}{eDT_{tp}-1} \right] \frac{eDT_{tp}}{eDT_{tp}-1}$$

Demand from abroad (imports):

$$da_{tp,t} = tD_{tp,t} dc_{tp,t} * \left(\frac{pc_{tp,t}}{pa_{tp,t}} \right)^{eDT_{tp}}$$

Demand from local:

$$dl_{tp,t} = (1 - tD_{tp,t}) dc_{tp,t} * \left(\frac{pc_{tp,t}}{pl_{tp,t}} \right)^{eDT_{tp}}$$

Demand value equation:

$$pc_{tp,t} dc_{tp,t} = pl_{tp,t} dl_{tp,t} + da_{tp,t} sa_{tp,t}$$

HWP markets

- transformation and mkt balance

Transformation:

$$dl_{pp,t} = \sum_{tp} a_{pp,tp,t} sl_{tp,t}$$

Primary products market balance:

$$\underbrace{sl_{pp,r} + sa_{pp,r} + \sum_{r2} rt_{pp,r2,r}}_{\text{production}} = \underbrace{dl_{pp,r} + sa_{pp,r} + \sum_{r2} rt_{pp,r,r2}}_{\text{reg. trade in}} = \underbrace{dl_{pp,r}}_{\text{cons.}} + \underbrace{sa_{pp,r}}_{\text{exp.}} + \underbrace{\sum_{r2} rt_{pp,r,r2}}_{\text{reg. trade out}}$$

supply *demand*

Transformed products market balance:

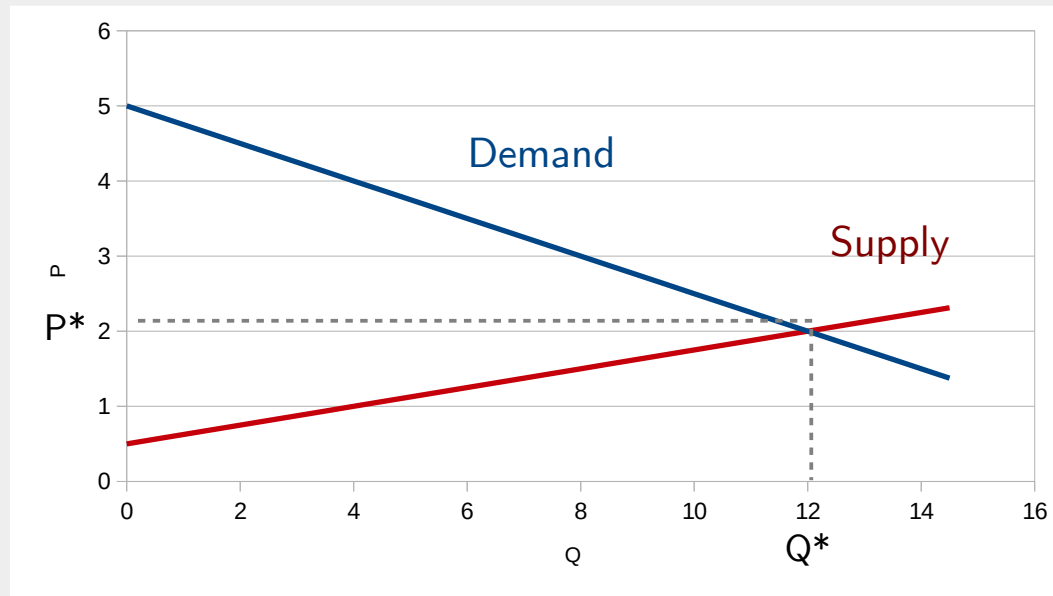
$$\underbrace{sl_{tp,r} + da_{tp,r} + \sum_{r2} rt_{tp,r2,r}}_{\text{prod.}} = \underbrace{dl_{tp,r} + da_{tp,r} + \sum_{r2} rt_{tp,r,r2}}_{\text{imp.}} = \underbrace{dl_{tp,r}}_{\text{consumption}} + \underbrace{\sum_{r2} rt_{tp,r,r2}}_{\text{reg. trade out}}$$

supply *demand*

Finding the equilibrium

- a possible implementation

- free markets
- linear forms of supply and demand functions



Q_D equal Q_S :

$$\begin{aligned} Q_D &= 20 - 4p \\ Q_S &= -4 + 8p \end{aligned}$$

(direct demand and supply functions)



$$20 - 4p = -4 + 8p$$



$$p^* = 2; Q^*_D = Q^*_S = 12$$

P_D equal P_S :

$$\begin{aligned} P_D &= -\frac{1}{4}Q + 5 \\ P_S &= \frac{1}{8}Q + \frac{1}{2} \end{aligned}$$

(inverse demand and supply functions)



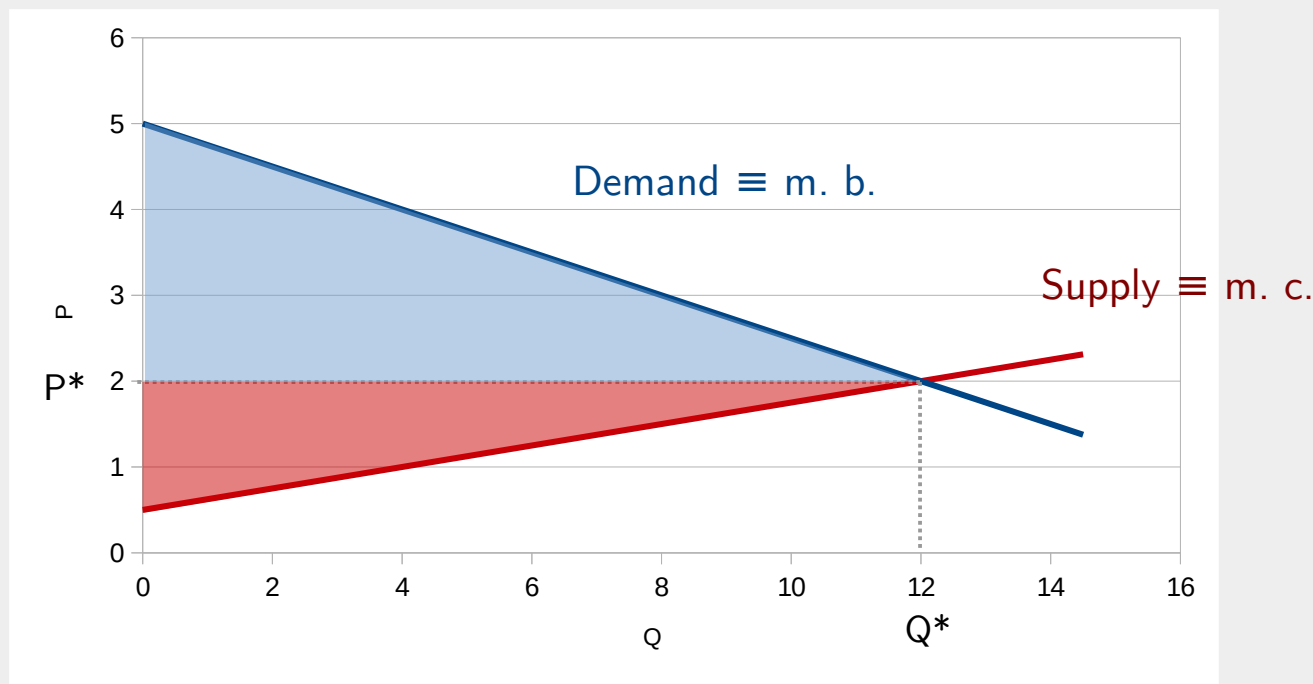
$$-\frac{1}{4}Q + 5 = \frac{1}{8}Q + \frac{1}{2}$$



$$Q^* = 12; P^*_D = P^*_S = 2$$

Market equilibrium

- the max surplus approach



$$\text{Consumer surplus} = \int_0^{Q^*} \left(-\frac{1}{4}Q + 5 \right) dQ - P^* Q^*$$

$$\text{Producer surplus} = P^* Q^* - \int_0^{Q^*} \left(\frac{1}{8}Q + \frac{1}{2} \right) dQ$$

$$\text{Total surplus} = \left[-\frac{1}{4} \frac{1}{2} Q^2 + 5Q \right]_0^{Q^*} - P_D^* Q^* + P_S^* Q^* - \left[\frac{1}{8} \frac{1}{2} Q^2 + \frac{1}{2} Q \right]_0^{Q^*} = -\frac{1}{8} Q^{*2} + 5Q^* - \left(\frac{1}{16} Q^{*2} + \frac{1}{2} Q^* \right)$$

$$\text{Max surplus} = \frac{d\text{Surplus}}{dQ^*} = 0 \rightarrow -\frac{1}{4} Q^* + 5 - \left(\frac{1}{8} Q^* + \frac{1}{2} \right) \rightarrow Q^* = 12; P_D^* = P_S^* = 2$$

Market equilibrium

- max surplus

```

Welcome Guide  market2.jl  market.jl  testset_3.jl  market_supersin  transp.jl  market.gms
1  using JuMP
2
3  # Qd = -da p + db
4  da = 4
5  db = 20
6  # Qs = sa p - sb
7  sa = 8
8  sb = 4
9
10 m = Model()
11
12 @variable(m, q >= 0)
13
14 @objective(m, Max, -(1/da)*(1/2)*q^2 + (db/da)*q - ((1/sa)*(1/2)*q^2+(sb/sa)*q))
15
16 print(m)
17
18 status = solve(m)
19
20 println("Objective value: ", getobjectivevalue(m))
21 println("q = ", getvalue(q))
22

```

Market module

- max surplus

Objective function: maximum total surplus

$$\sum_{tp,r} \left[\int_0^{dc_{tp,r}} pc_{tp,r} \{dc_{tp,r}\} d dc_{tp,r} - pc_{tp,r} * dc_{tp,r} \right]$$

transformed products consumers surplus

$$+ \sum_{pp,r} \left[pc_{pp,r} * sc_{pp,r} - \int_0^{sc_{pp,r}} pc_{pp,r} \{sc_{pp,r}\} d sc_{pp,r} \right]$$

primary products producers surplus

$$+ \sum_{tp,r} sl_{tp,r} * pl_{tp,r} - \sum_{tp,r} ac_{tp,r} * sl_{tp,r} - \sum_{pp,r} dl_{pp,r} * pl_{pp,r}$$

domestic transformers (revenues - tr. costs - costs)

$$+ \sum_{prd,r,r2} (pl_{prd,r2} - pl_{prd,r} - tc_{prd,r,r2}) rt_{prd,r,r2}$$

regional trader's surplus

Market module

- constraints

$$sl_{pp,r} + sa_{pp,r} + \sum_{r2} rt_{pp,r2,r} - (dl_{pp,r} + sa_{pp,r} + \sum_{r2} rt_{pp,r,r2}) = 0$$

primary products material balance

$$sl_{tp,r} + da_{tp,r} + \sum_{r2} rt_{tp,r2,r} - (dl_{tp,r} + da_{tp,r} + \sum_{r2} rt_{tp,r,r2}) = 0$$

transformed products material balance

$$\frac{sc_{pp,t}}{sc_{pp,t-1}} - \left(\frac{pc_{pp,t}}{pc_{pp,t-1}} \right)^{eSP_{pp}} \left(\frac{inv_{pp,t}}{inv_{pp,t-1}} \right)^{eSI_{pp}} = 0$$

composite supply f(composite price)

$$\frac{dc_{tp,t}}{dc_{tp,t-1}} - \left(\frac{pc_{tp,t}}{pc_{tp,t-1}} \right)^{eDP_{tp}} = 0$$

composite demand f(composite price)

$$sc_{pp,t} - \left[(1 - tS_{pp,t}) sl_{pp,t}^{\frac{eST_{pp}-1}{eST_{pp}}} + tS_{pp,t} sa_{pp,t}^{\frac{eST_{pp}-1}{eST_{pp}}} \right]^{\frac{eST_{pp}}{eST_{pp}-1}} = 0$$

composite supply def. from local and abroad supplies

$$dc_{tp,t} - \left[(1 - tD_{tp,t}) dl_{tp,t}^{\frac{eDT_{tp}-1}{eDT_{tp}}} + tD_{tp,t} da_{tp,t}^{\frac{eDT_{tp}-1}{eDT_{tp}}} \right]^{\frac{eDT_{tp}}{eDT_{tp}-1}} = 0$$

composite demand def. from local and abroad demands

$$sa_{pp,t} - tS_{pp,t} sc_{pp,t} * \left(\frac{pc_{pp,t}}{pa_{pp,t}} \right)^{eSt_{pp}} = 0$$

exports

$$da_{tp,t} - tD_{tp,t} dc_{tp,t} * \left(\frac{pc_{tp,t}}{pa_{tp,t}} \right)^{eDt_{tp}} = 0$$

imports

$$pc_{pp,t} sc_{pp,t} - (pl_{pp,t} sl_{pp,t} + pa_{pp,t} sa_{pp,t}) = 0$$

value balance of composite price prim. products

$$pc_{tp,t} dc_{tp,t} - (pl_{tp,t} dl_{tp,t} + da_{tp,t} sa_{tp,t}) = 0$$

value balance of composite price transf. products

Market module

- summary

As result of surplus maximisation we have:

- quantities of primary products (pp) and transformed products (tp) supplied, demanded, imported, exported and regionally-traded in each region;
- prices of pp and tp in each region.

Prices for pp → used in the allocation module

Supply of pp → used in the forest resource dynamic module

Some other aspects we didn't saw:

- supply also from death timber (timber from mortality event in the forest dynamic module);
- supply of specific transformed products (fuelwood) also as by-product of transformation of other transformed products;
- as national products are homogeneous, prices in the various regions differ only by transport costs
→ we can study spillover effects



AREA ALLOCATION MODULE

Forest investment decisions

- FFSM implementation (area allocation module)

- **Area allocation module:** agent based micro-economic model; area allocation endogenised; regeneration = f ($\pi(\text{prices, growth, mortality})$); forest managers heterogeneous for (a) managed forest resources, (b) degree of risk-aversion (prices and growth vs. mortality), (c) level of expectations (observed vs. future prices, growth, mortality);
- Forest investments are chosen based (comparing) on the SEV (WTP for amenities) .
- Two corrections are made before the comparison:
 - Transaction costs are subtracted from the SEV. These transaction costs are defined for each couple of *current forest type, compared forest type*.
 - As (a) forest investments involve a certain risk, (b) this risk is different for the different investments, and (c) the aversion for the risk is different for the various managers, the comparison is carried on over a certain equivalent SEV of the investment, computed as:

$$CESEV_{i,j} = SEV_i * (1 - ra_j * cumMort_i)$$

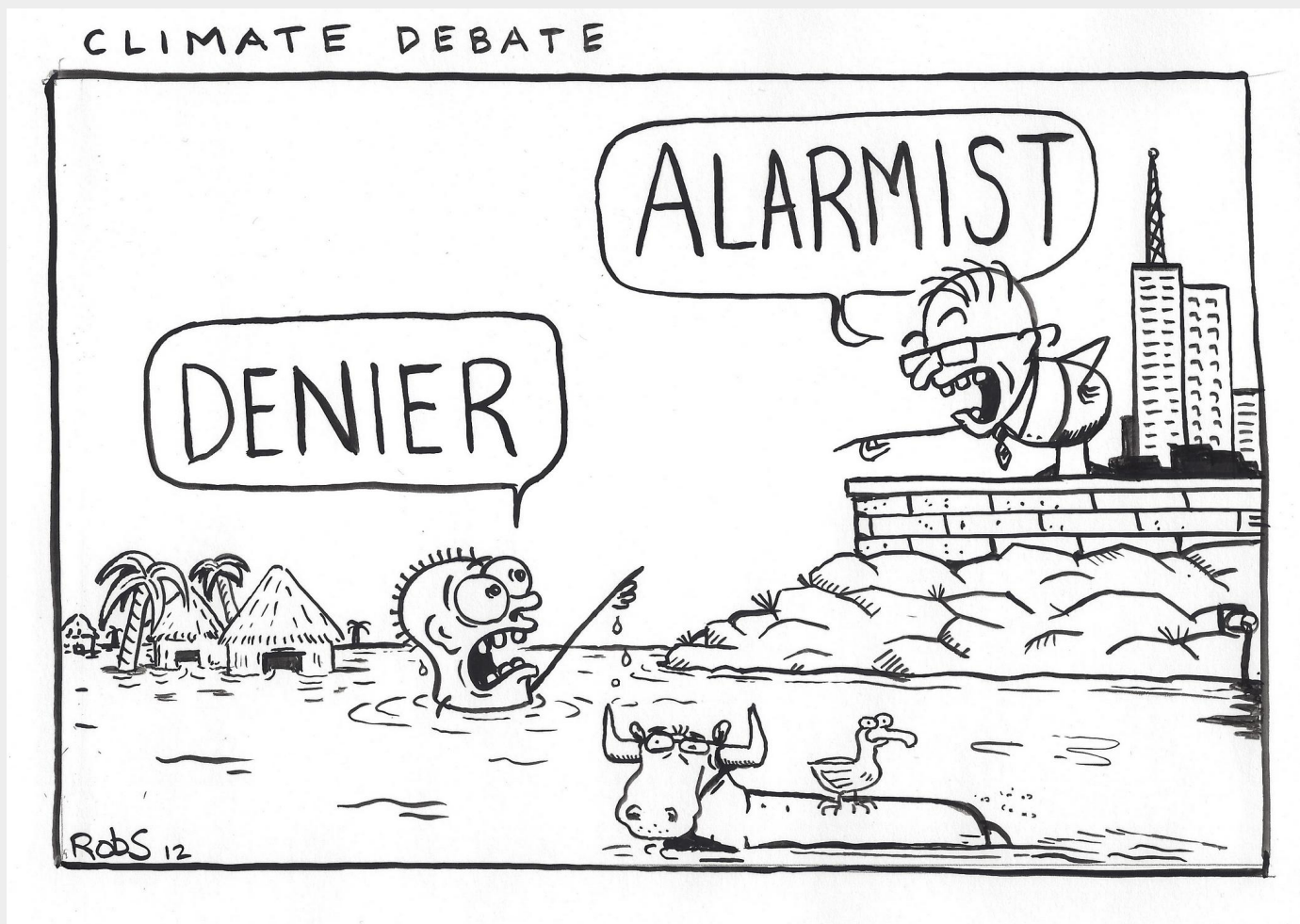
where $CESEV_{i,j}$ is the certain equivalent SEV of forest investment i for the forest manager j , SEV_i is the original SEV, ra_j is the risk aversion coefficient for forest manager j and $cumMort_i$ is the average cumulative mortality expected for forest investment i before maturation.

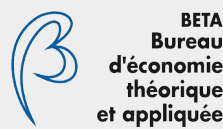
- Future mortality and growth rates needed to compute the SEV can be those forecasted by the specific scenario or can be those prevailing at time to make the investment, depending from forest manager expectations

Forest investment decisions

- FFSM implementation (area allocation module)

Heterogeneous expectations are important as.. we don't all have the same opinion about climate change !

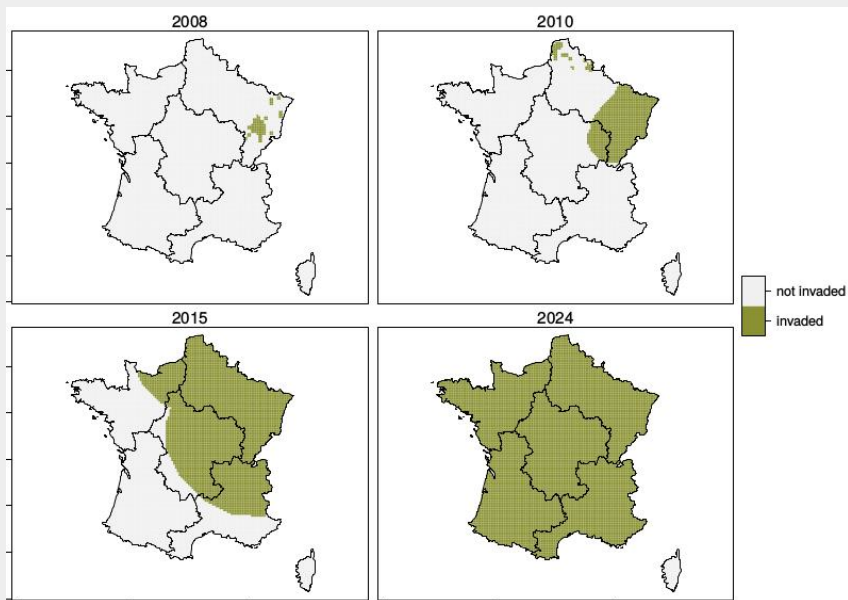




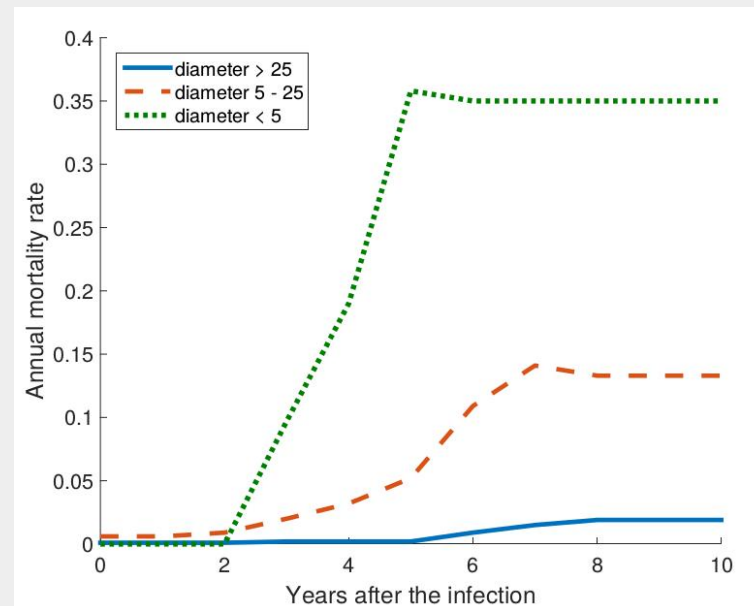
PATHOGEN MODULE

Forest resources

- pathogen module



Exogenous spread model of a pathogen (ash dieback here)



Increased mortality for specific px, ft, dc as a function of time of presence of the pathogen

Results:

- strong resource and market impact (up 80% less ash with the pathogen than without it);
- spillover effects: (temporary) benefits for the regions not yet involved, and benefits for the markets of other species;
- effect for ash owners depends strongly on the degree of substitutability between ash and other broadleaved;
- forest owner “economic adaptation” may further reduce ash presence.



CARBON BALANCE MODULE

Climate change

- impact on the forest sector

Physical impact

- Δ growth by so-called CO₂ "fertilisation" (maybe)
- Δ growth and Δ mortality by
 - direct effect (drought, fires, storms..)
 - indirect effect (fungi, insects, pests in general)

Quel rôle pour les forêts et la filière forêt-bois françaises dans l'atténuation du changement climatique ?

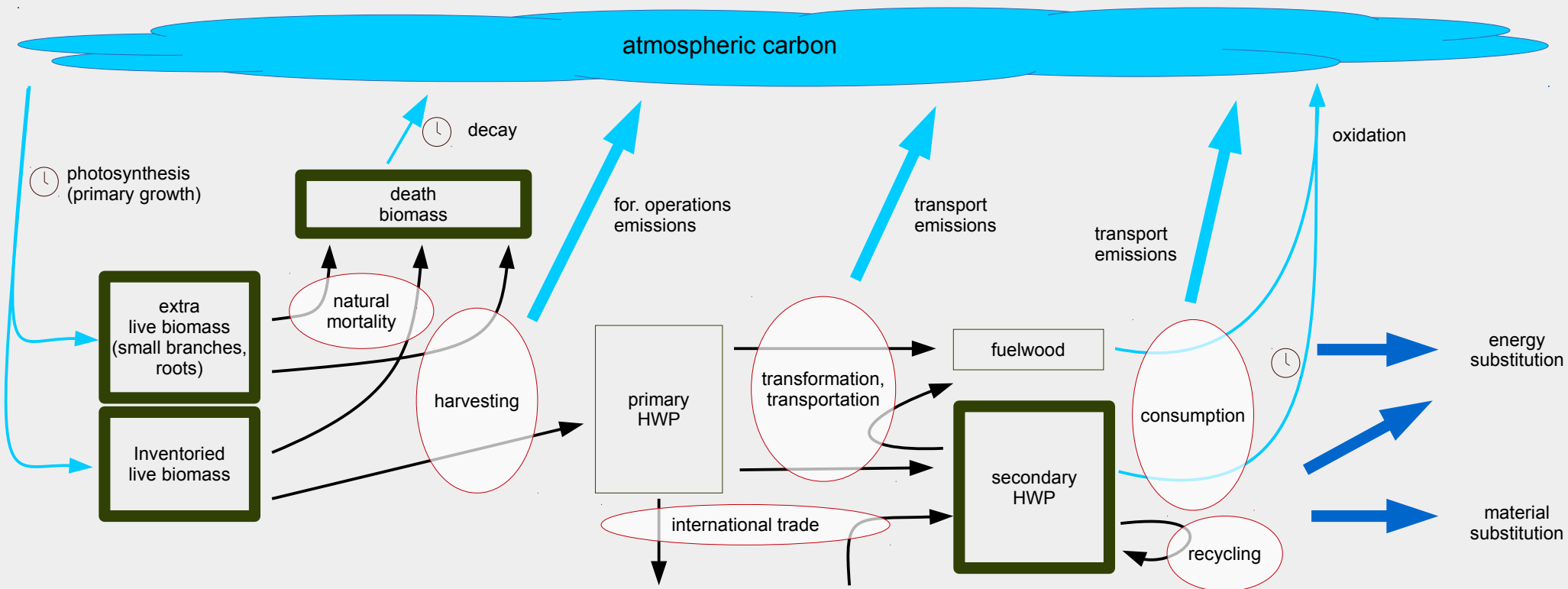
- Rapport d'étude pour le Ministre de l'Agriculture et de l'Alimentation

Market impact

- international wood prices impacted by cc induced variation in the wood supply and demand and in the competition of wood with other materials

Carbon module flowchart

- **Carbon module:** “registers and accounts” forest and forest sector carbon emitted/sequestered/substituted;



Squares: carbon pools; ellipses: processes. The clock icon denotes multi-period flows. Elements accounted for in the module are drawn using wider contours.

Events handled by the carbon module

Event	Affected pool and direction
harvesting	cumEmittedForOper(+), forestPool(-)
wood production	woodProductsPool(+), cumSubstitutedEmissions(+)
wood transportation	cumEmittedForOper}(+)
forest growth	forestPool(+)
disturbance events	forestPool(alive: -; death: +)
(time passing)	forestPool(death: -), woodProductPool(-)



DATA

Data

- Spatial, temporal and forest type/dc automatic override – go as specific as you can!
- When we don't have data... we use scenarios/sensitivity analysis/MonteCarlo sampling
- Forest resource module:
 - forest static inventory data for initial year (volumes by ft, dc and region)
 - forest land cover GIS layer
 - forest dynamic inventory data for initial year ($E[\text{growth, mortality}]$ and $\text{var}(\text{growth, mortality})$ by ft, dc, region)
 - CC: scenario-specific modifiers of $\{\text{growth, mortality}\}$ by ft, dc, region|pixel
- Marked module:
 - initial demand/supply/trade/prices of HWP per product, region
 - supply, demand and trade (Armington) elasticity per product
 - initial and subsequent years international prices of HWP
- Area-allocation module:
 - $E[\text{risk aversion coefficient, expectation coefficient}]$, $\text{var}(\text{risk aversion coefficient, expectation coefficient})$
 - management rate by region
- Carbon module
 - inventory vs whole tree/roots/soil expansion factors
 - carbon sequestration coefficients
 - carbon substitution coefficients



RESULTS SUMMARY

Results

- background

Some results from a recent paper that “sum up” our latest work with the model for analysis of climate change impacts to give an overview of which could be the long-term impacts for the forest sector (up to a century).

For this study FFSM++ itself has been coupled with a statistical model of forest response to climate change and a statistical land-use model to deal with competition of forest activities with agricultural ones.

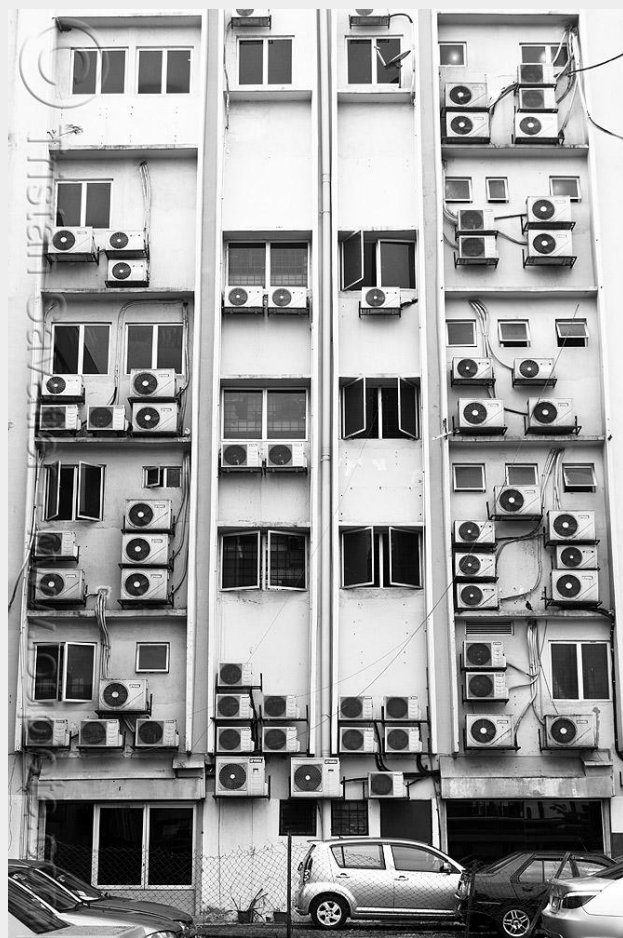
Entry points of the climate change cascade of impacts modelled are climatic anomalies and variations in international prices for timber products.

Delacote P., Lobianco A., Caurla S., Bontemps J.D., Lungarska A., Mérian P., Rivière M., Barkaoui A. (2021), “[The loop effect: how climate change impacts the mitigation potential of the French forest sector](#)”, *Journal of Forest Economics*, 36(3)

Climate change

- the "loop" effect

Can we model mitigation and adaptation independently ?



Do our adaptation strategies have any influence on the mitigation? Or, in other words, does adaptation pose some limits on the possibilities we have to mitigate?

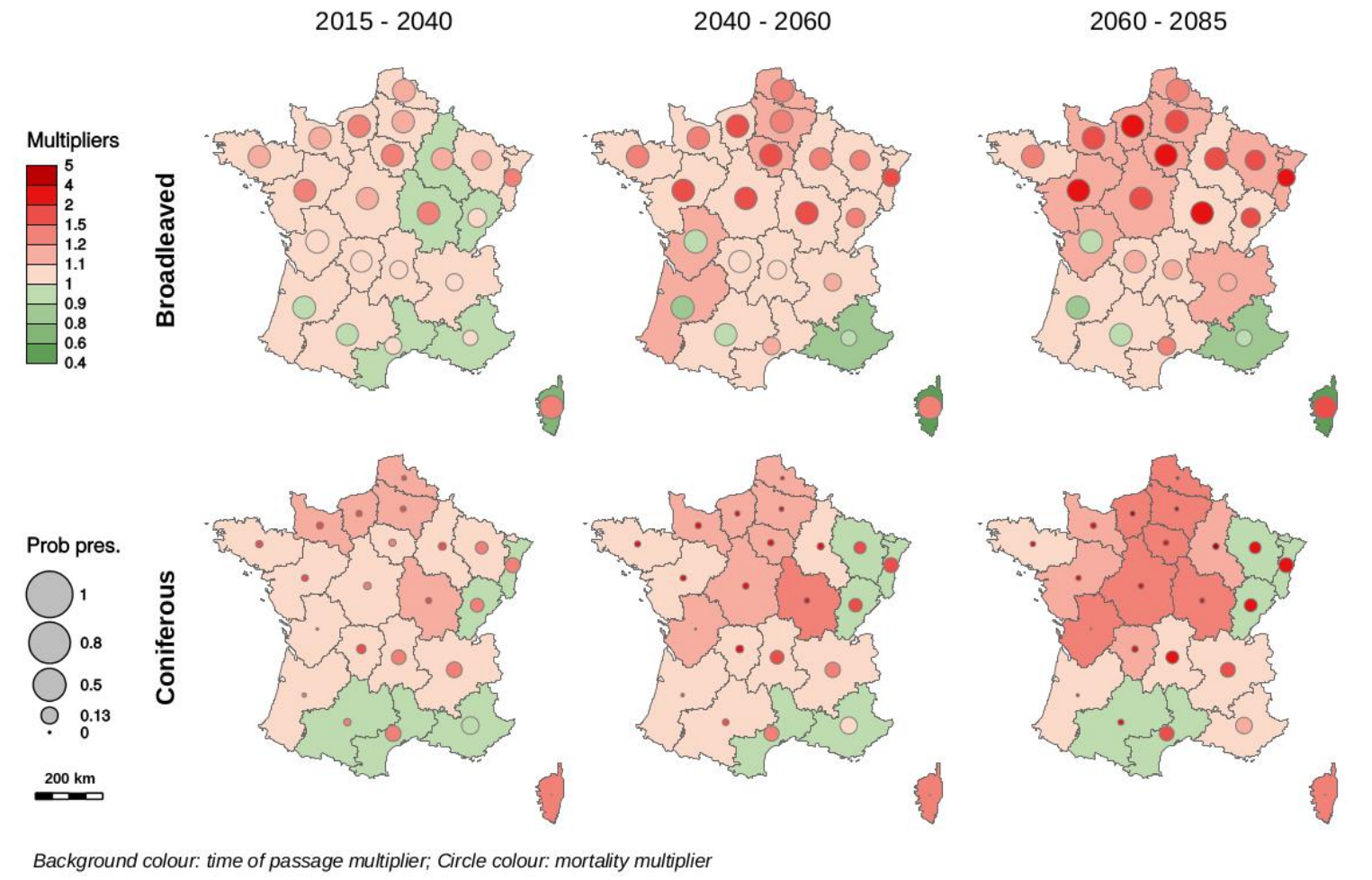
2022, Increased energy use for adaptation significantly impacts mitigation pathways

Nature Communications

Results

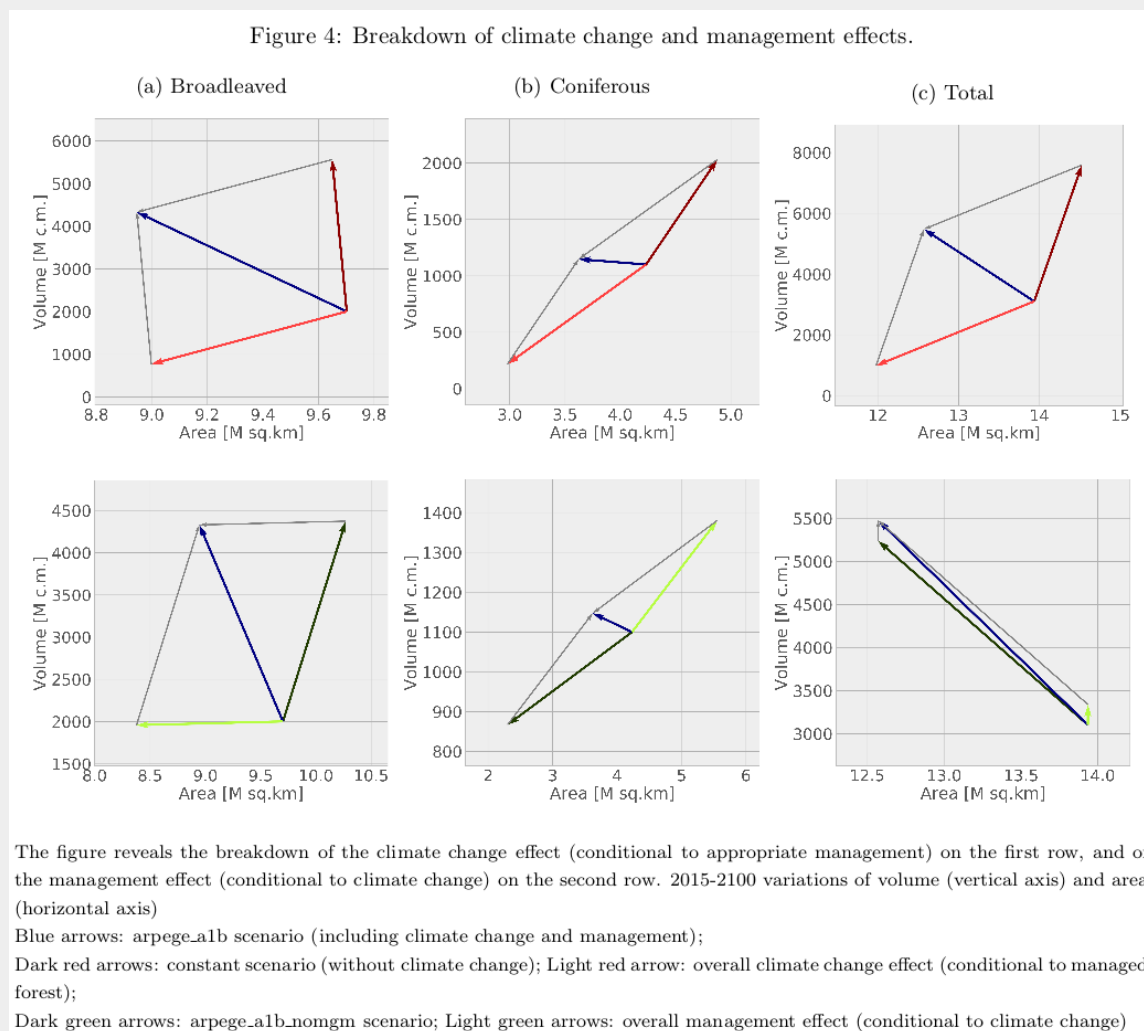
Climate change impacts on tree's mortality are more important than those on tree's growth variations;

Figure 2: Direct effects of climate change: time of passage (between diameter classes) multipliers, mortality multipliers and probabilities of presence.



Results (2)

Climate change impact is more strong on coniferous species compared to broadleaved ones, and its effect may be strong enough to override substantial profit-driven preferences for coniferous forests by forest managers;



Results (3)

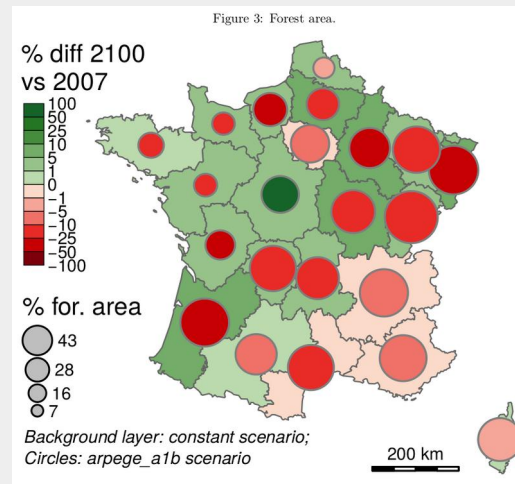
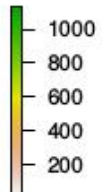
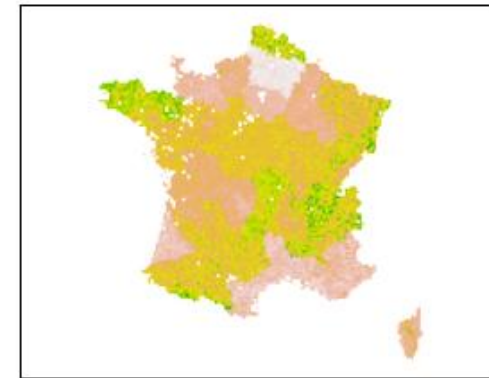
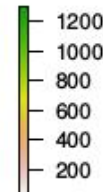
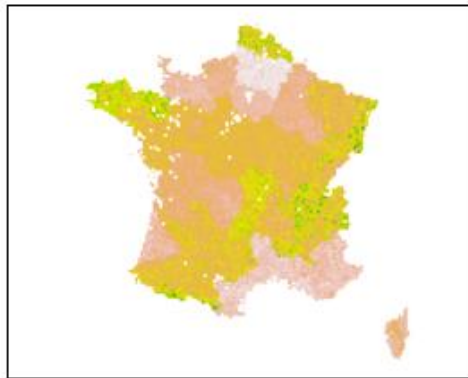
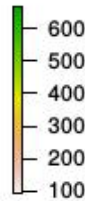
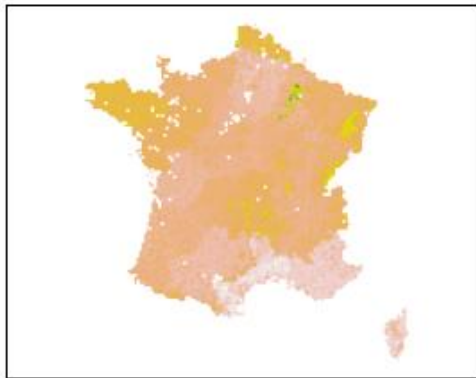
Despite an increase in harvesting intensity, primarily driven by increased international prices for harvested wood products, and increasing climate change impacts, the forest resource continue to expand in terms of volumes, but in terms of area they reduces;

Forest volume density (m^3/ha)

2015

a1b, 2100

a1b_nomgm, 2015



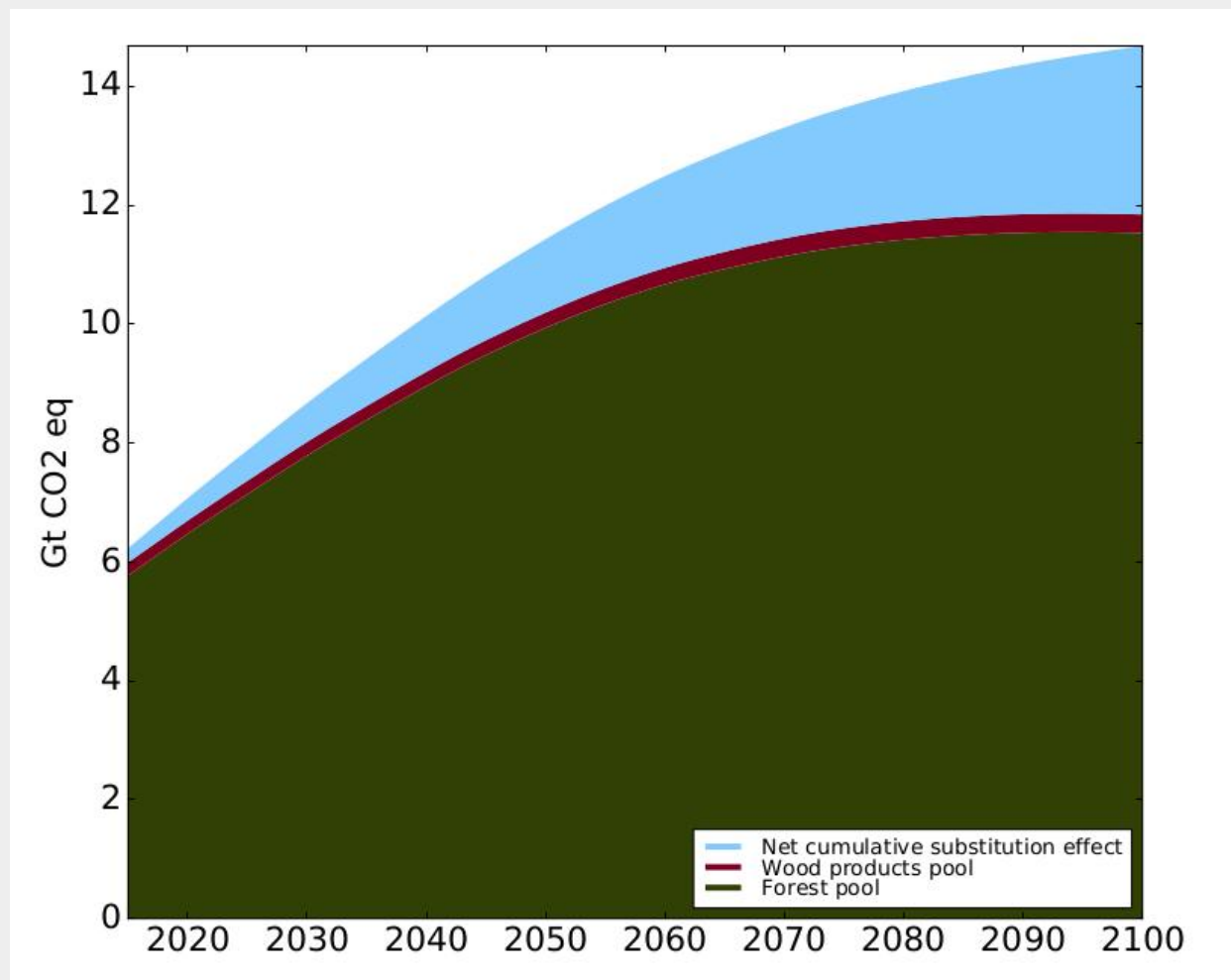
Results (4)

- (a) Despite an increase in harvesting intensity and increasing climate change impacts, forest resources continue to expand;
- (b) Due to the long term horizon of forest investments, future climate change impacts already have strong consequences on today's forest investment profitability;
- (c) The expansion of harvesting wood products markets advantage both producers (+89.9% in producer's surplus) and consumers (+12.0%);
- (d) Forest sector mitigation potential is estimated at 123 Mt CO₂eq/y (94.7 Mt CO₂eq/y from sequestration and 28.4 94.7 Mt CO₂eq/y from substitution);

Results (5)

The forest capacity to provide sequestration opportunities for atmospheric carbon is strongly declining with time and it ceases around 2070-2080;

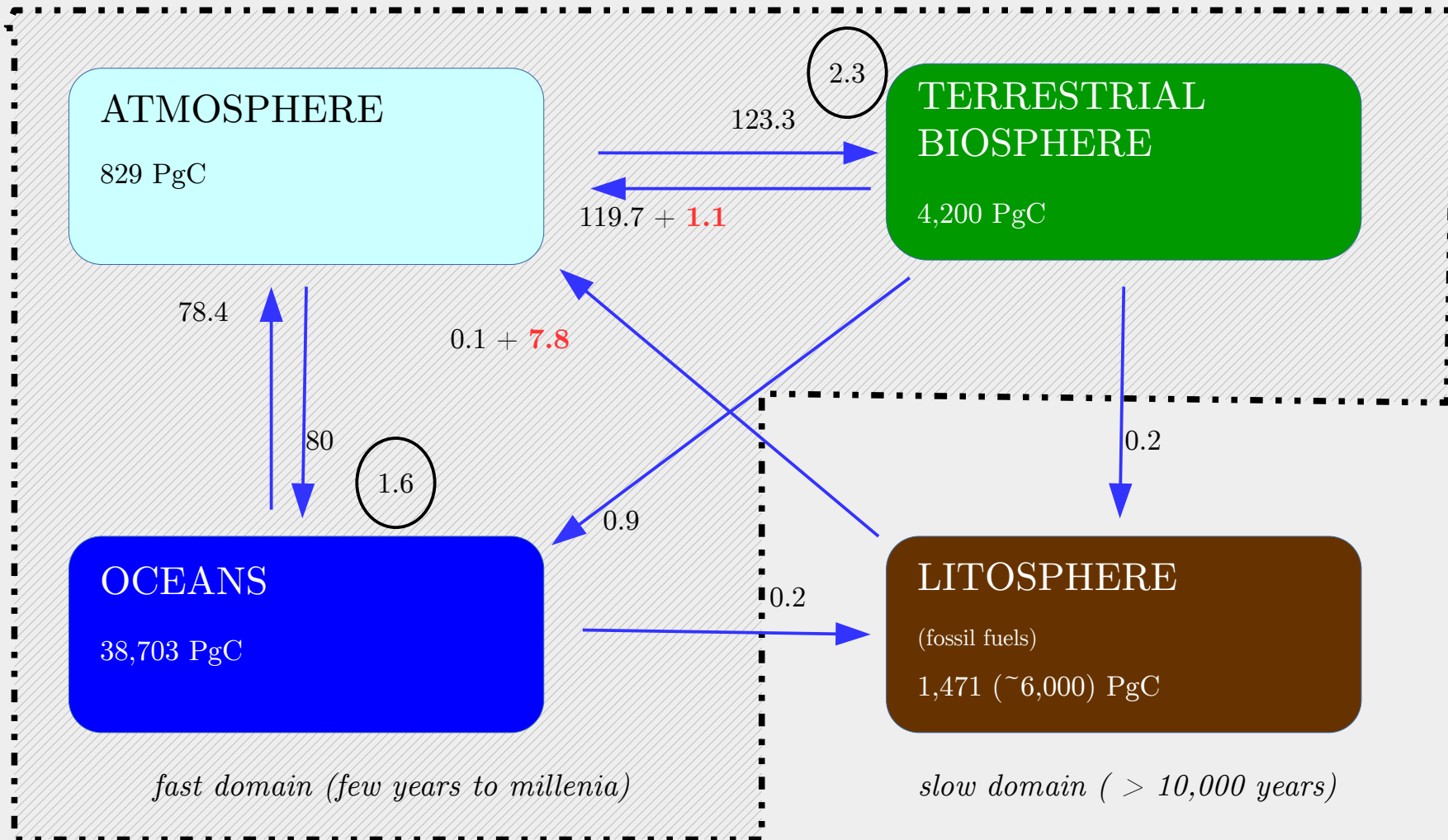
Dynamics of the carbon balance



In line with the increasing scientific evidence that the pool is becoming saturated – hence it will be less able in the future to absorb additional CO2 from the atmosphere.

Climate change

- forest mitigation potential

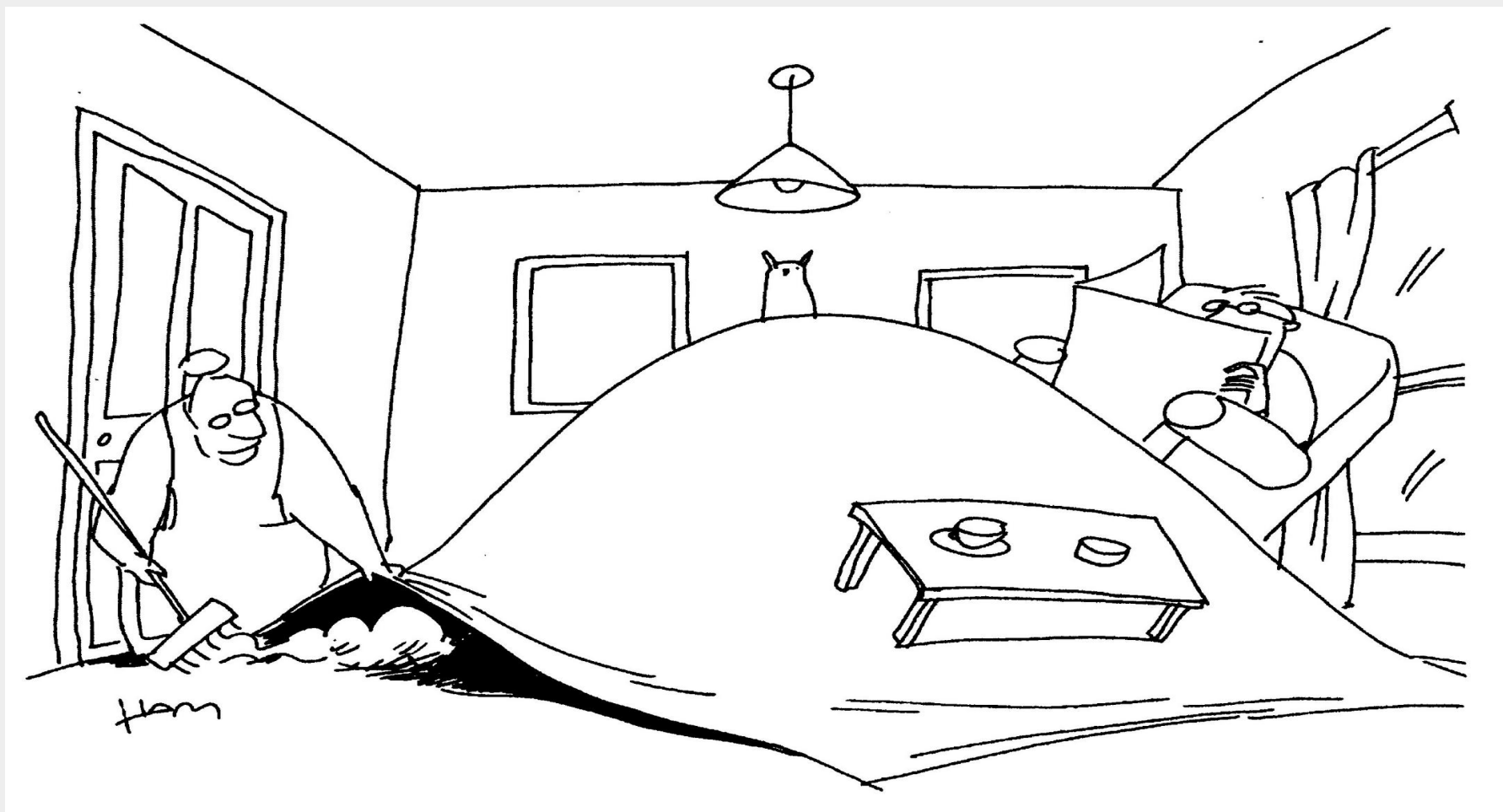


Source: Lobianco et al. (2016), adapted from Ciais and Sabine (2013)

Climate change

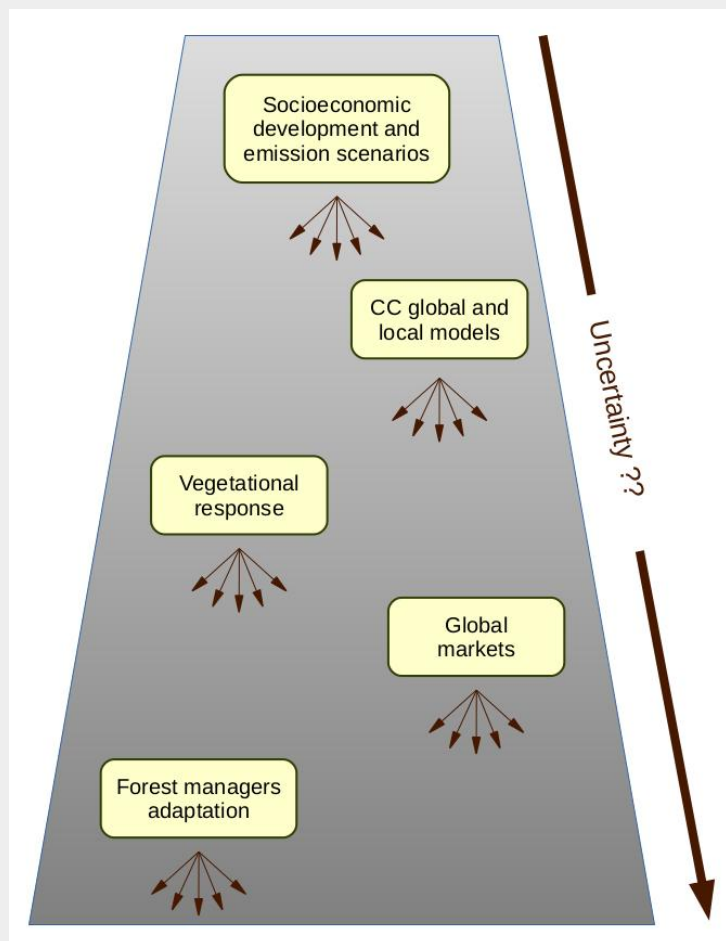
- forest mitigation potential

Storing carbon in the terrestrial biosphere, within the fast domain sinks is a bit like *sweeping the dirt under the carpet*



Results (6)



Uncertainty derived from employing different climatic models over the same IPCC storyline has the same order of magnitude than the uncertainty derived from employing the same climatic model under different storylines.



Climate change

- forest mitigation potential

Q removal

appropriate, removals , and how... 5		United Nations	FCCC/CP/2015/L.9/Rev.1
and removals in accordance wit... 5			
or removals in their nationally d... 5			
or removals are excluded; 32. D... 5			
and removals by sinks covered b... 6			
and removals by sinks of greenh... 22		Framework Convention on Climate Change	Distr.: Limited 12 December 2015
and removals corresponding to ... 23			Original: English
and removals , Parties should ta... 23			
and removals by sinks of greenh... 29			

Conference of the Parties
Twenty-first session
Paris, 30 November to 11 December 2015

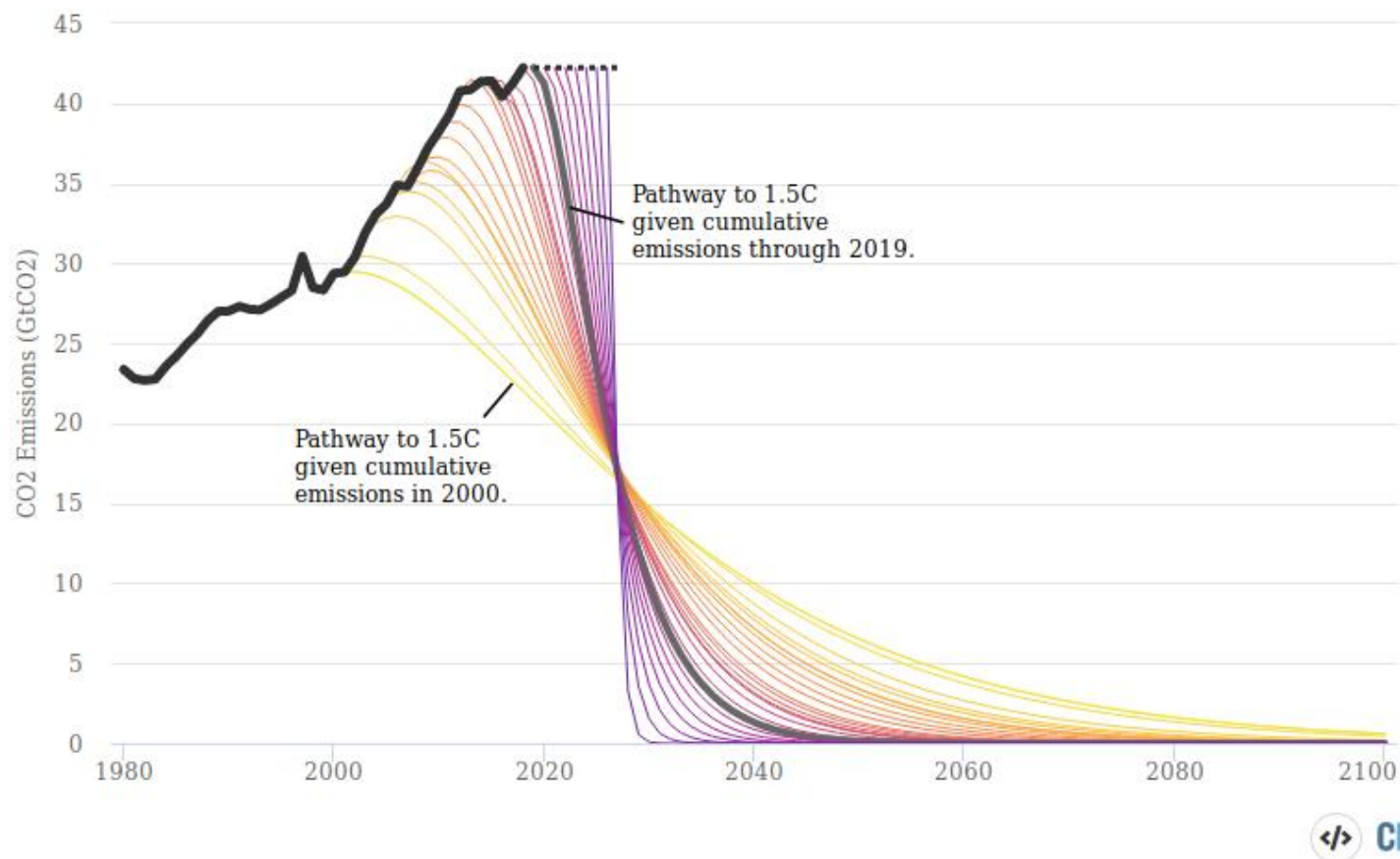
Agenda item 4(b)
Durban Platform for Enhanced Action (decision 1/CP.17)
**Adoption of a protocol, another legal instrument, or an
agreed outcome with legal force under the Convention
applicable to all Parties**

ADOPTION OF THE PARIS AGREEMENT

Proposal by the President

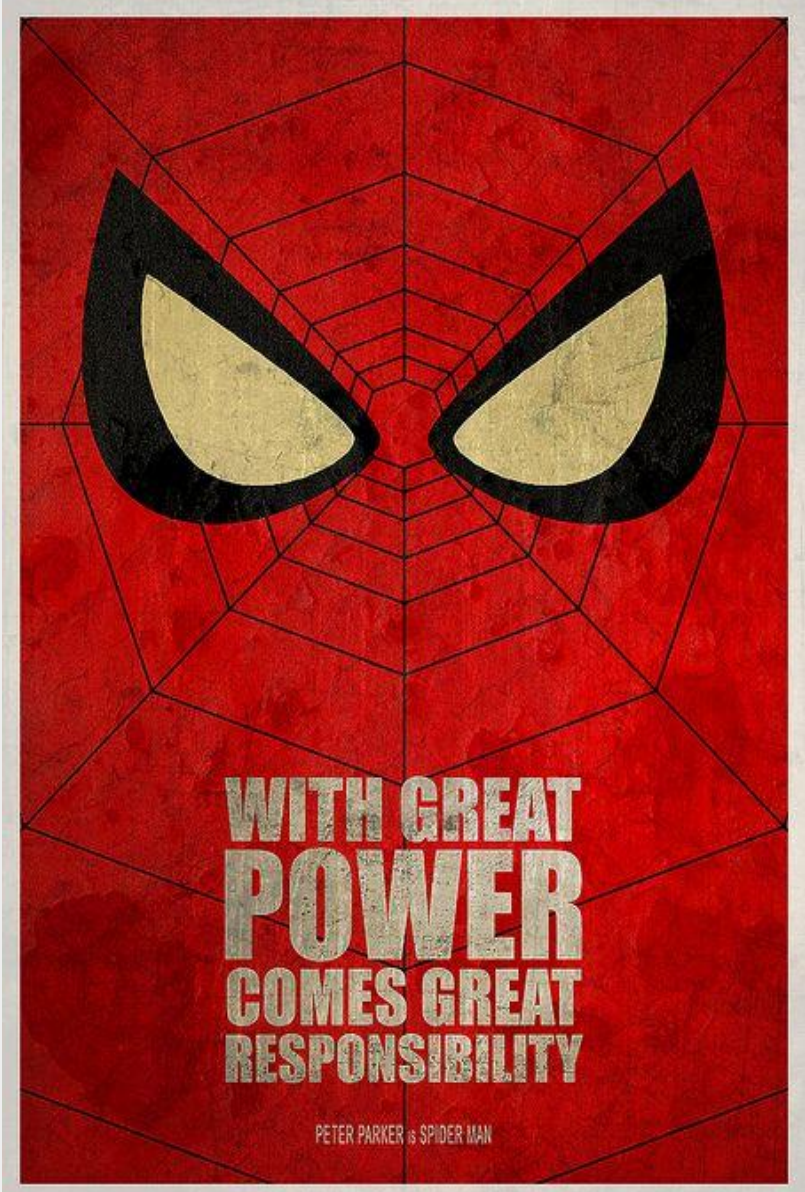
Draft decision -/CP.21

Limiting warming to 1.5C increasingly difficult without large-scale negative emissions



Emission reduction trajectories associated with limiting warming below 1.5C by starting year. Solid black line shows historical emissions, while dashed black line shows emissions constant at 2018 levels. Source: Historical CO2 emissions from the [Global Carbon Project](#). 1.5C carbon budgets based on the [IPCC SR15 report](#). Original figure from [Robbie Andrews](#). Chart by Carbon Brief using [Highcharts](#).

The forest sector will save the world !



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- FFSM development team



<http://ffsm-project.org>



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